



# **Validation of Heat Transfer Correlations in Line Chill-down Tests of Cryogenic Fluid in SINDA/FLUINT**

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- Line chill-down is an important process in cryogenic tank propellant management, storage, and usage
- Complex flow dynamics during these processes:
  - boiling heat transfer (film, transition, and nucleate)
- Understanding boiling phenomena can lead to efficient line chill-down systems that use less propellant, propellant stored, reducing cost for space missions

- Line Chill-down heat transfer was modelled using SINDA/FLUINT version 5.8 (SF)
- Multiple chill-down tests were modelled using:
  - heat transfer correlations readily available in SF using HTN/HTC TIES
  - heat transfer empiricisms developed by the University of Florida (UF) based on a series of liquid nitrogen chill-down tests using SF HTU TIES
- Chill-down tests modelled:
  - liquid nitrogen tests conducted by the University of Florida
    - horizontal flow, upward flow, and downward flow (Reynolds Numbers ranging 850 – 231,000)
  - liquid hydrogen tests conducted by NASA Glenn Research Center
    - vertical upward flow (Reynolds Number range of 18,400 – 433,000)

## SF Heat Transfer Methodology

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If  $T_{wall} > T_{dffb}$ , then
    Use  $h = h_{fb}$ 
Else
    Calculate  $T_{leid}$ 
    If  $T_{wall} > T_{leid}$ , then
        Use  $h = h_{fb}$ 
    Else
        Calculate  $q''_{CHF}$ 
        Calculate  $q''_{nb}$  based on  $h_{nb}$ 
        If  $q''_{nb} > q''_{CHF}$ , then
            Use  $h = h_{tb}$  based on  $T_{wall}$ ,  $T_{leid}$ ,  $T_{CHF}$ 
        Else
            Use  $h = h_{nb}$ 
        End if
    End if
End if
 $h_{boil} = h$ 
If subcooled boiling ( $T_{wall} > T_{sat}$  but  $T < T_{sat}$  and  $X=0$ ), then
    Calculate  $h_{liq}$ , the liquid film coefficient based on all liquid (full FR) and Dittus-Boelter
    Update  $h$  by interpolation between  $h_{boil}$  and  $h_{liq}$  based on
Else if Dry ( $X > X_{nb}$ ), then
    Update  $h$  by interpolation between  $h_{boil}$  and  $h_{vap}$  based on  $X$ 
End if
    
```

SINDA FLUENT Boiling Heat Transfer Calculation Summary for HTN Ties:

$X$  is the flow quality (may or may not be lump quality), and FR is the mass flow rate

Calculate  $h_{nb}$ , the nucleate boiling coefficient, using the CHEN correlation at a quality of  $\text{MIN}(X, X_{nb})$

Calculate  $h_{vap}$ , the vapor film coefficient, at a flow rate of  $X \cdot FR$  using Dittus-Boelter correlation

Calculate  $h_{fb}$ , the film boiling coefficient using  $h_{vap}$  if it is greater than  $h_{fb}$

Calculate  $T_{dffb}$ , departure of film boiling temperature, roughly  $0.9 \cdot T_{cr}$

## UF Heat Transfer Methodology

Calculate  $T_{wet}$  prediction for the given mass flow rate and local pressure

A If  $T_w > T_{wet}$  then  $h = h_{fb}$

B If  $T_w < T_{wet}$ , then:

1. If  $T_w > T_{sat}$ , then:

a) Calculate  $q''_{CHF}$  prediction

b) Calculate  $q''_{nb}$  prediction

i) If  $q''_{nb} > q''_{CHF}$  then  $h = h_{tb}$

ii) If  $q''_{nb} < q''_{CHF}$  then  $h = h_{nb}$

2. If  $T_w < T_{sat}$  then  $h = h_{DB}$

Figure 1: Heat Transfer Methodology

UF Film Boiling Correlation:

$$Nu = c_1 \left[ 1 + \left( \frac{1}{\frac{L}{D} + 0.1} \right)^{c_2} \right] \left( \frac{GD}{\mu_v} \right)^{c_3} \text{Pr}_v^{c_4} \text{erf} \left( \frac{X_E + 1}{\log_{c_5} \text{Re}_v} \right)^{c_6} \left( \frac{\mu_v}{\mu_{v,\text{wall}}} \right)^{c_7} \\ + c_8 \left( \frac{k_l}{k_v} \right) \exp \left( - \left( \frac{L}{D} \right)^{c_9} \right) \underbrace{We_D^2 \left[ \frac{h_{fg}}{c_{p,v}(T_w - T_{\text{sat}})} \right]}_{\text{Weber number, } G^2 D / (\rho_l \sigma)}$$

SF film boiling uses a correlation by Bromley for low quality flows\*:

$$U_{\text{FB}} = 0.62 \left[ \frac{k_v^3 \rho_v g (\rho_l - \rho_v) (h_{fg} + 0.4 C_{p,v} \Delta T)}{L_h \cdot \mu_v \Delta T} \right]^{\frac{1}{4}}$$

Diameter for external flow  
Or MIN (Diameter/2, hemholtz instability,  $L_h$ ) for internal flow

$$L_{h,\text{max}} = 8.646 \left[ \frac{\sigma^4 \cdot h_{fg}^3 \cdot \mu_v^5}{\rho_v \cdot (\rho_l - \rho_v)^5 \cdot g \cdot k_v^3 \cdot \mu_v \cdot \Delta T^3} \right]^{\frac{1}{11}}$$

\*For higher quality flows a correlation by Groeneveld is used making sure the minimum is a least vapor Dittus-Boelter



UF Nucleate Boiling Correlation:

$$h_{nb} = c_1 \text{Pr}_l^{c_2} \text{Ja}^{c_3} \text{We}_D^{c_4} \left[ \frac{\rho_l g (\rho_l - \rho_v) D^3}{\mu_l^2} \right]^{c_5} h_{sp,l}$$

$$h_{sp,l} = 0.023 \frac{k_l}{D} \text{Re}_l^{0.8} \text{Pr}_l^{0.4}$$

$$q_{CHF}'' = c_1 G h_{fg} \text{We}_L^{-0.5} \left( \frac{\rho_l}{\rho_v} \right)^{-0.91} \left( \frac{L}{D} \right)^{0.48} \left( 1 + 0.07 \text{We}_L^{0.35} \frac{\Delta h_{sub}}{h_{fg}} \right)$$

UF Transition Boiling Correlation:

$$h_{tp} = c_0 \text{Pr}_l^{c_1} X h_{nb}$$

$$X = 10.37 - 36.93 \theta + 47.49 \theta^2 - 20.82 \theta^3$$

$$\theta = \frac{T_w - T_{sat}}{T_{wet} - T_{sat}}$$

$$T_{wet} = \frac{27}{32} T_{cr} (1 + c_1 \text{We}_D^{c_2} \text{Re}_l^{c_3} \text{Ja}^{c_4})$$

SF nucleate boiling uses the Chen correlation, and transition boiling is a nonlinear interpolation between nucleate and film boiling

# Liquid Nitrogen Line Chill-down



LN<sub>2</sub> was pressurized, subcooled, and supplied from a storage Dewar

LN<sub>2</sub> pool cooler used to preserve subcooling from the Dewar

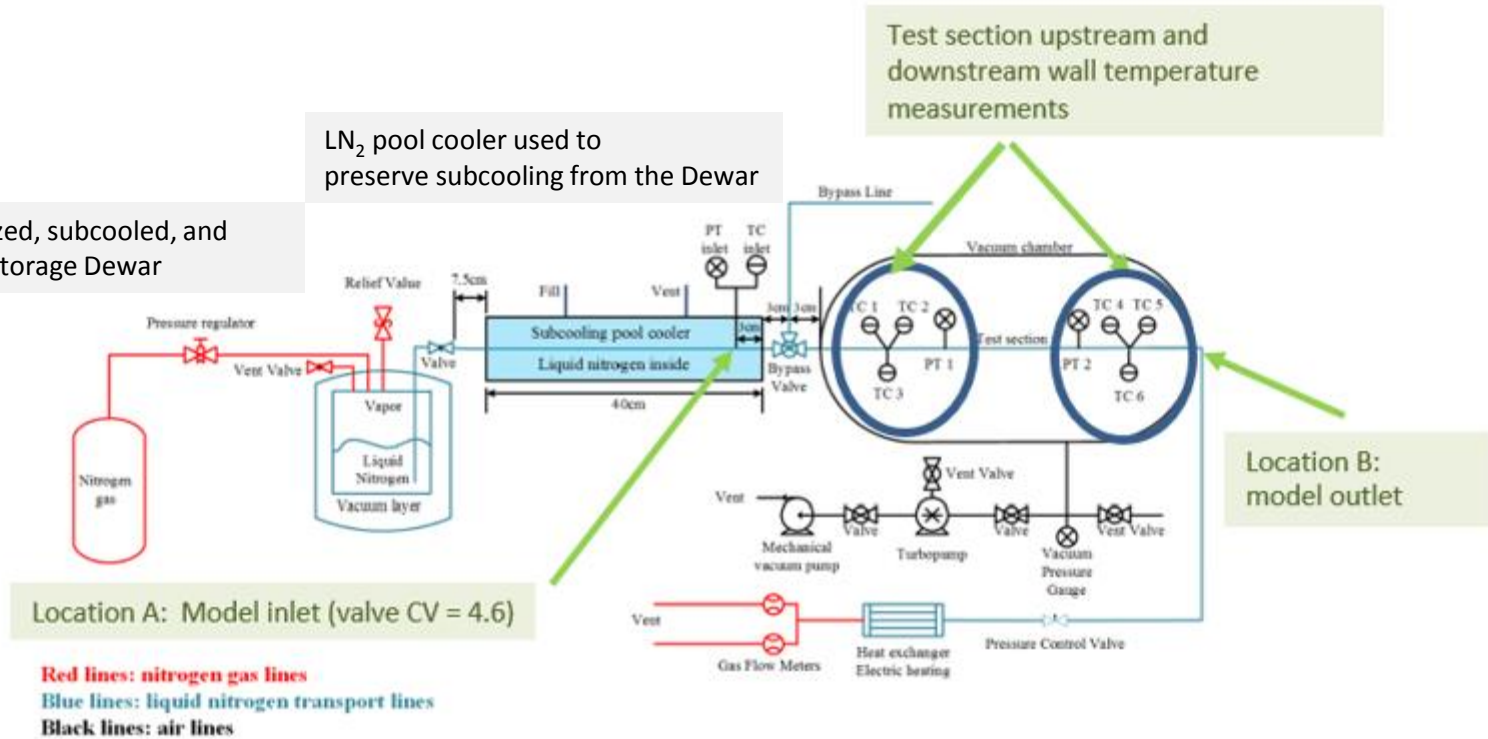
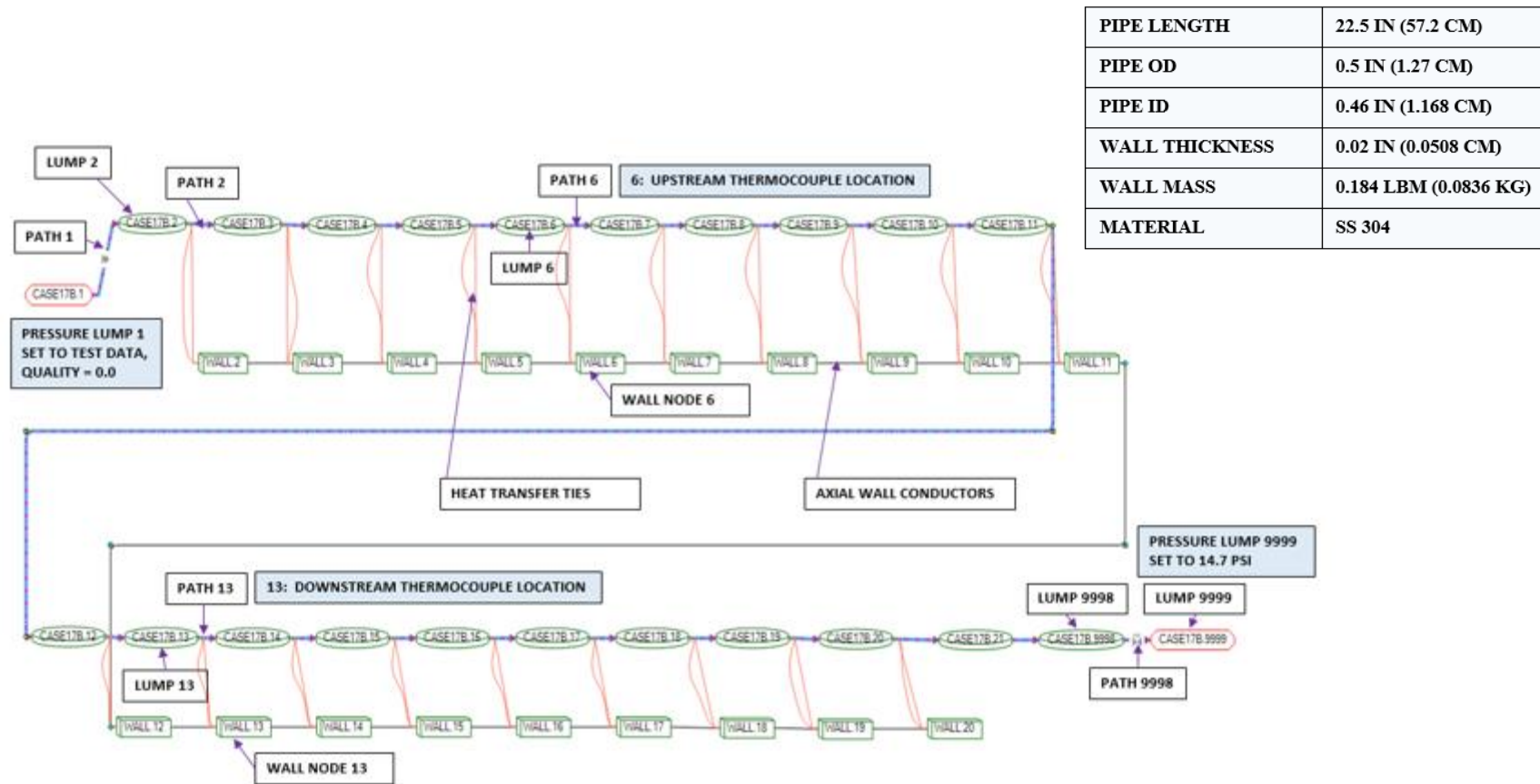


Figure 2: Liquid Nitrogen Chill-down Test Schematic

# Liquid Nitrogen Line Chill-down



**Figure 3: SINDA/FLUINT Flow Schematic of the Liquid Nitrogen Test Section Showing Fluid LUMPS, Flow PATHS, Wall NODES, Heat Transfer TIES, and Pipe Axial CONDUCTORS**





The flow rate was measured far downstream of the test section, near the system exit. Where to set the flow rate?

- SF was highly sensitive, and sometime unstable, setting the test flow rate downstream (the outlet) of the test section model and setting the test pressure upstream (the inlet) of the test section model
  - higher flow rate oscillations at the entrance of the model's test section
- SF was more stable setting the test flow rate upstream (than the downstream flow rate set case)
  - test pressure was used as an inlet (SF plenum) to set the thermodynamic state (temperature and quality) coming into the system
  - setting the appropriate downstream pressure was the unknown



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  - setting the appropriate downstream pressure was the unknown



The pressure drops predicted by SF for the downstream set flow rate boundary condition were much smaller than test section measured pressure drops

- The multiphase pressure drop correlations used internally in SF may need to be adjusted
- Models with an upstream flow rate set assumed a pressure drop that was small

# Liquid Nitrogen Line Chill-down Results (Horizontal Flow)

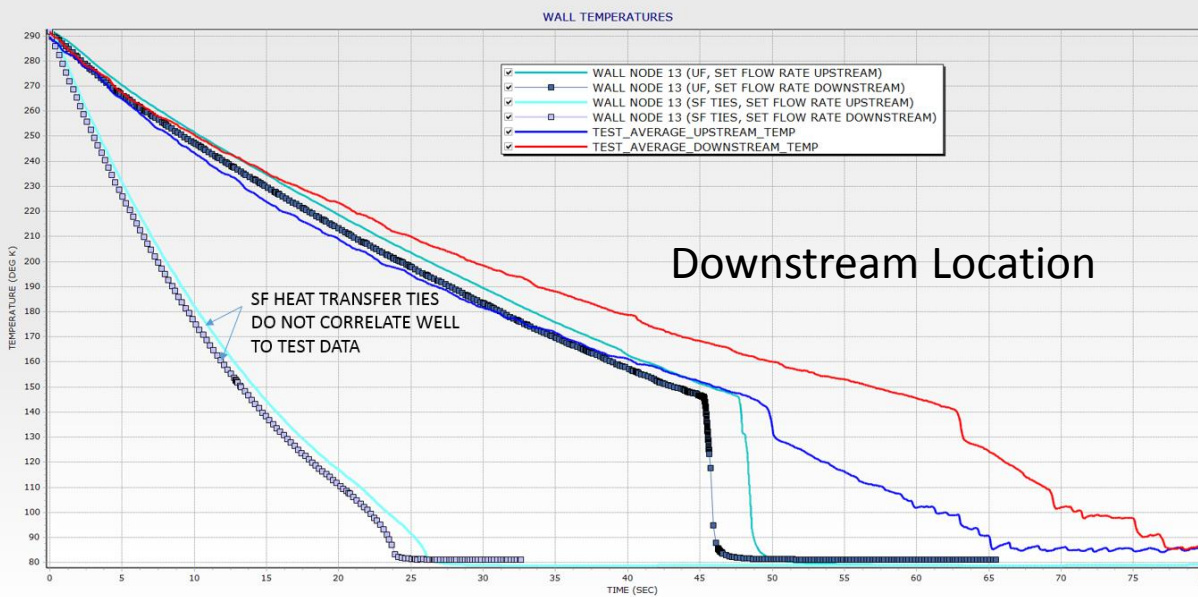
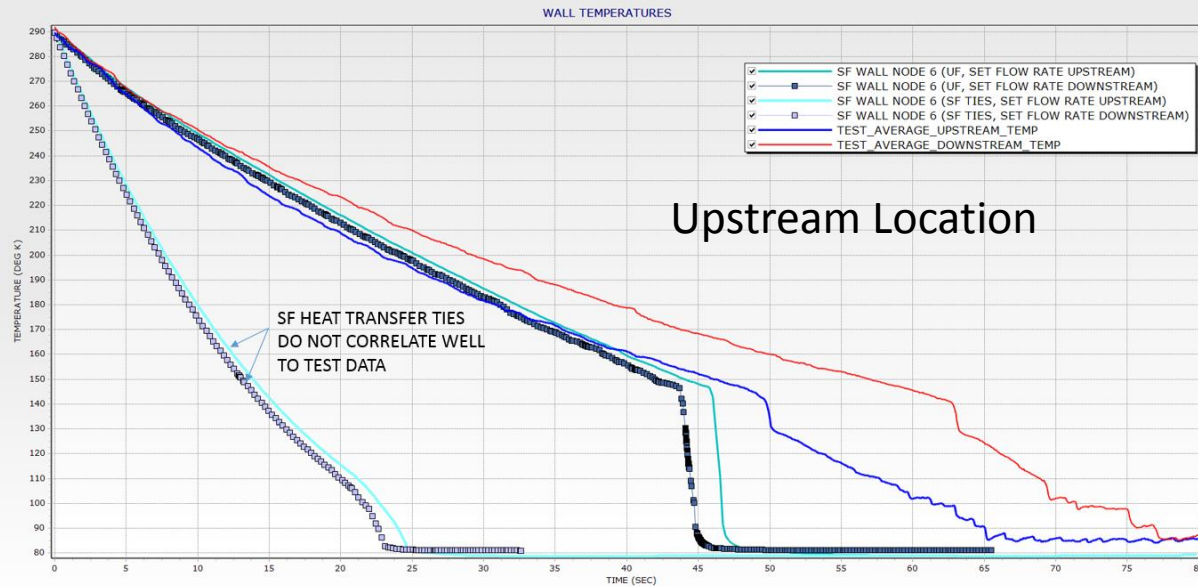
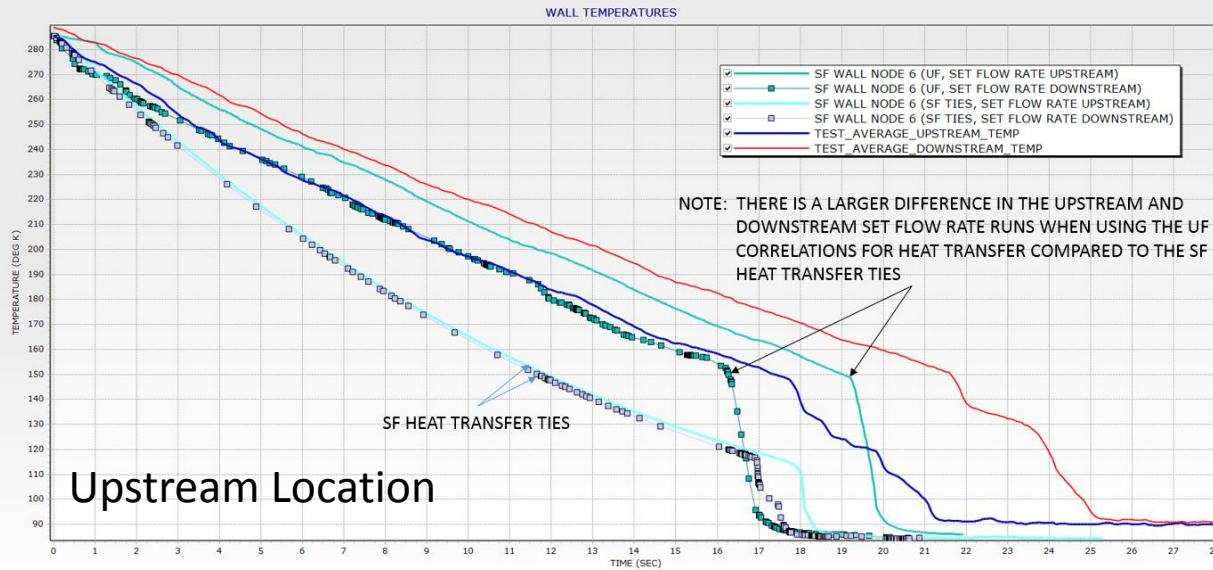


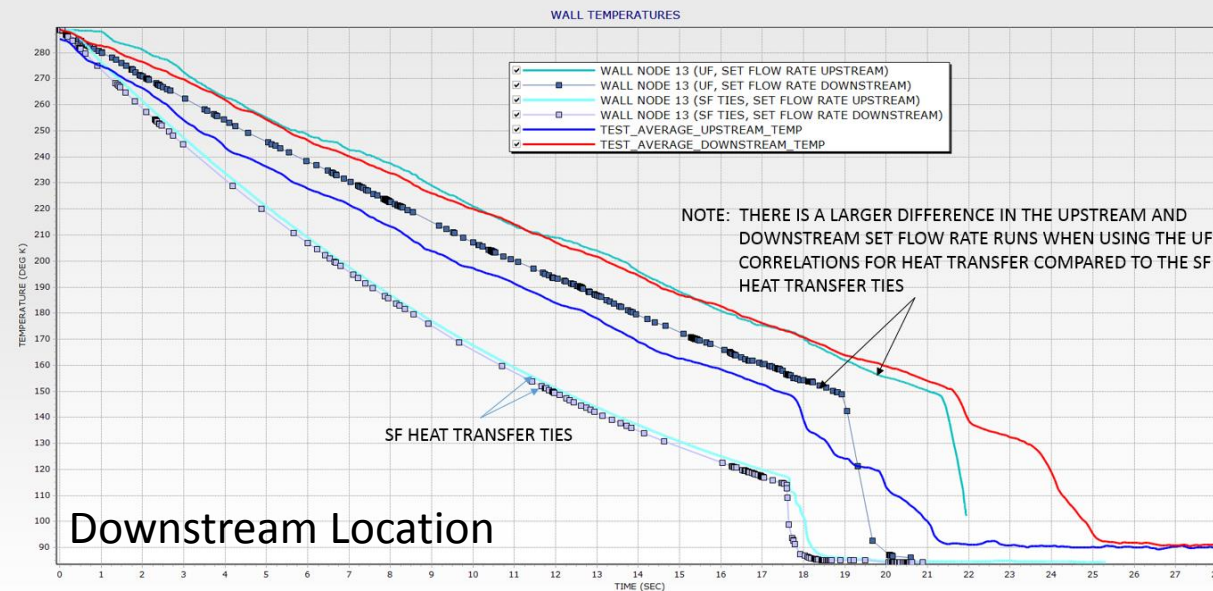
Figure 4a-4b: Wall Temperatures for Liquid Nitrogen Horizontal Chill-down Test Case Reynolds Number = 3743



# Liquid Nitrogen Line Chill-down Results (Horizontal Flow)

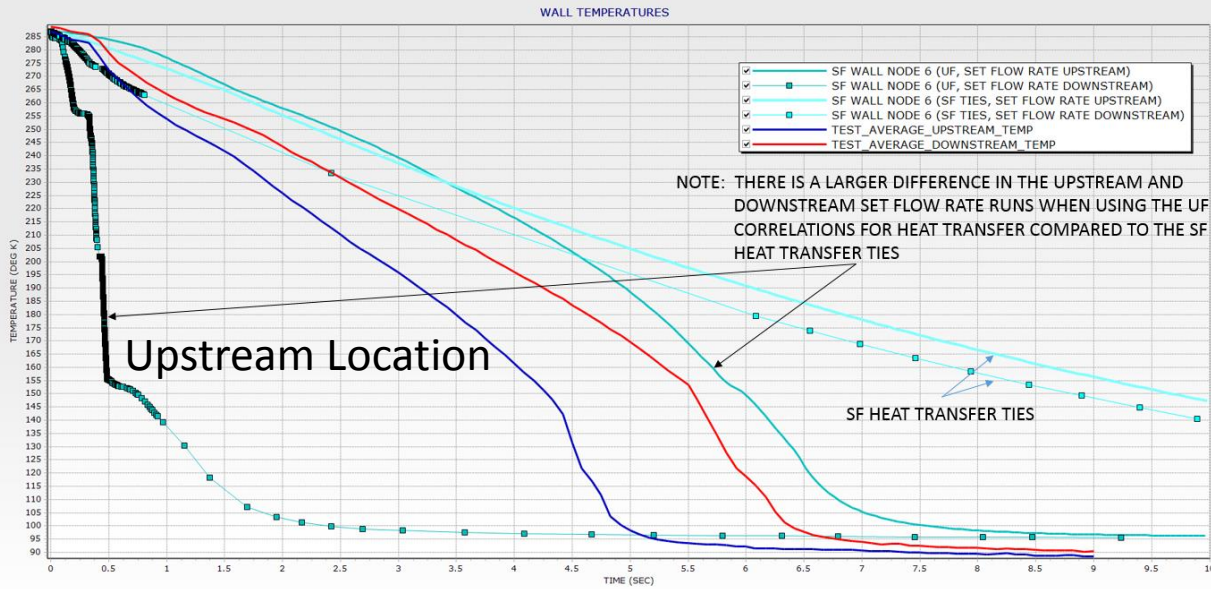


**Figure 5a-5b: Wall Temperatures for Liquid Nitrogen Horizontal Chill-down Test Case Reynolds Number = 23677**

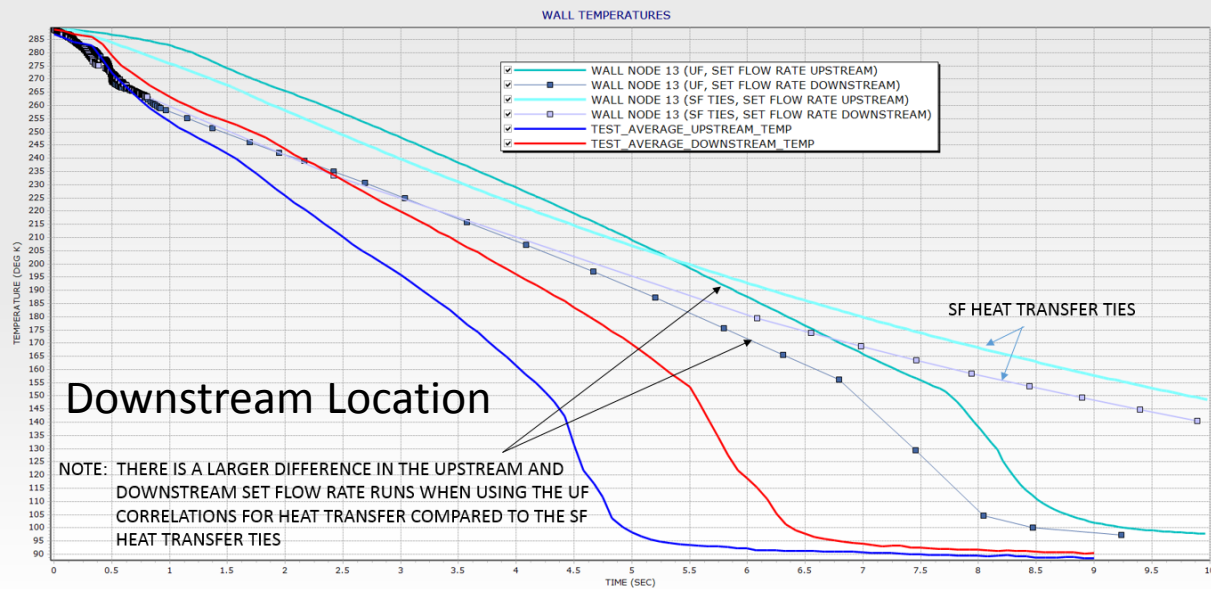




# Liquid Nitrogen Line Chill-down Results (Horizontal Flow)



**Figure 6a-6b: Wall Temperatures for Liquid Nitrogen Horizontal Chill-down Test Case Reynolds Number = 132597**



# Liquid Nitrogen Line Chill-down Results (Horizontal Flow)

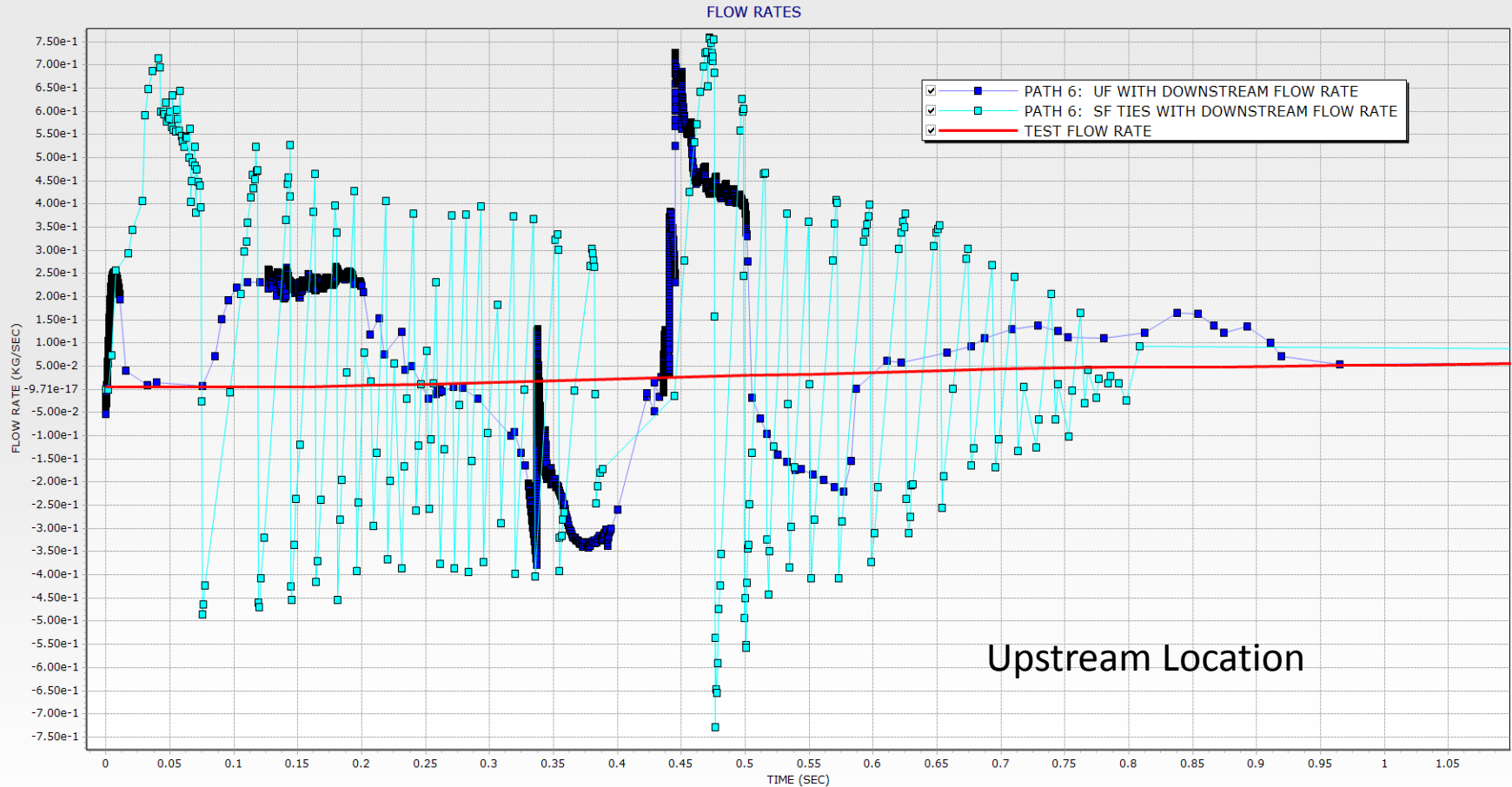
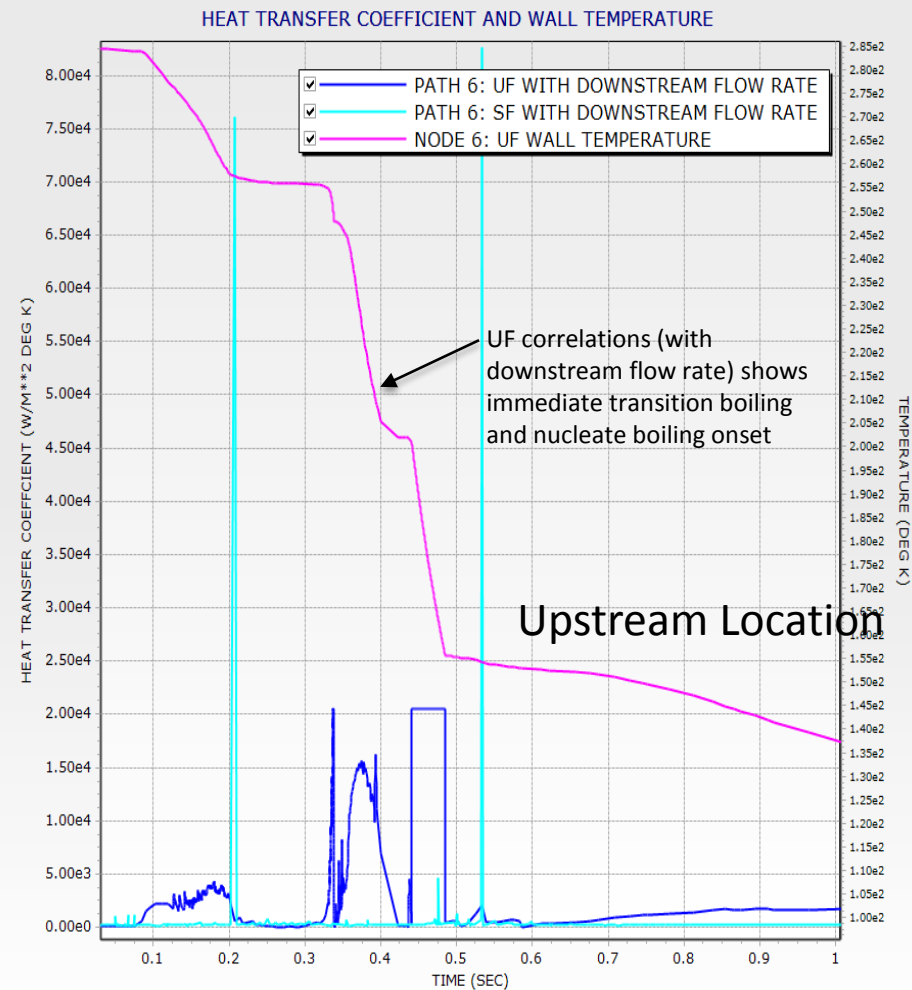
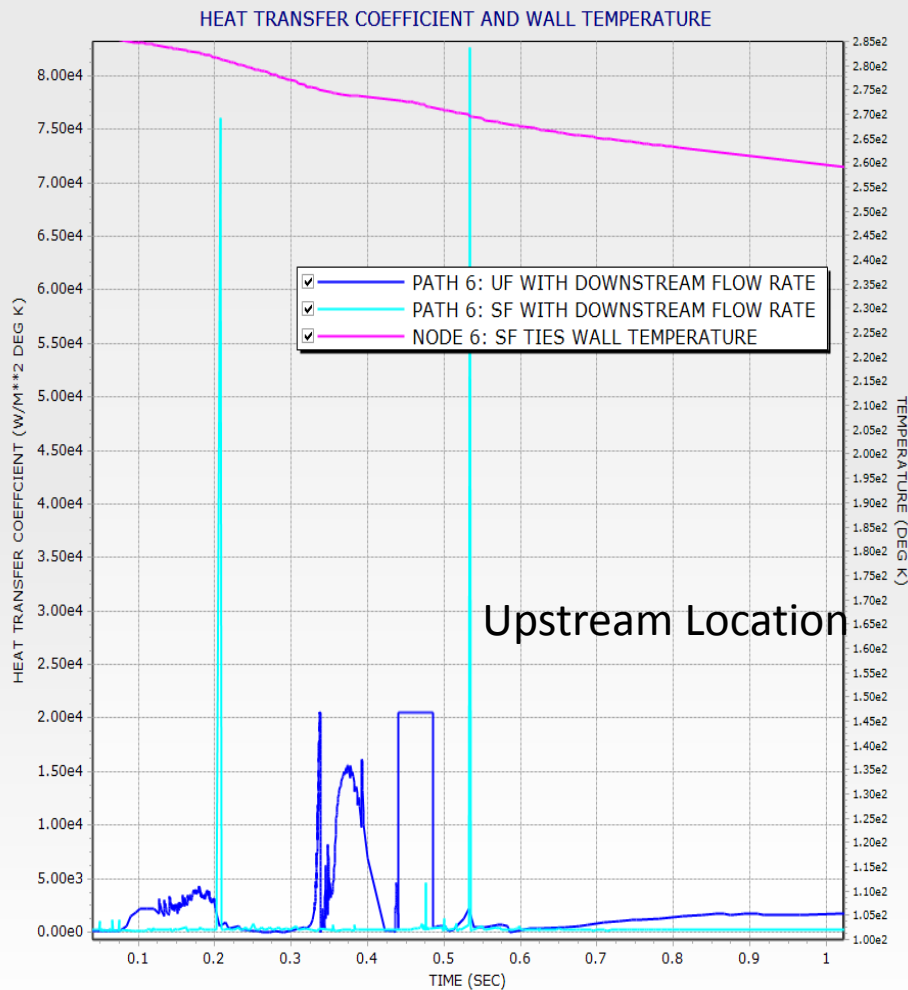


Figure 7: Liquid Nitrogen Horizontal Chill-down Test Case Reynolds Number = 132597

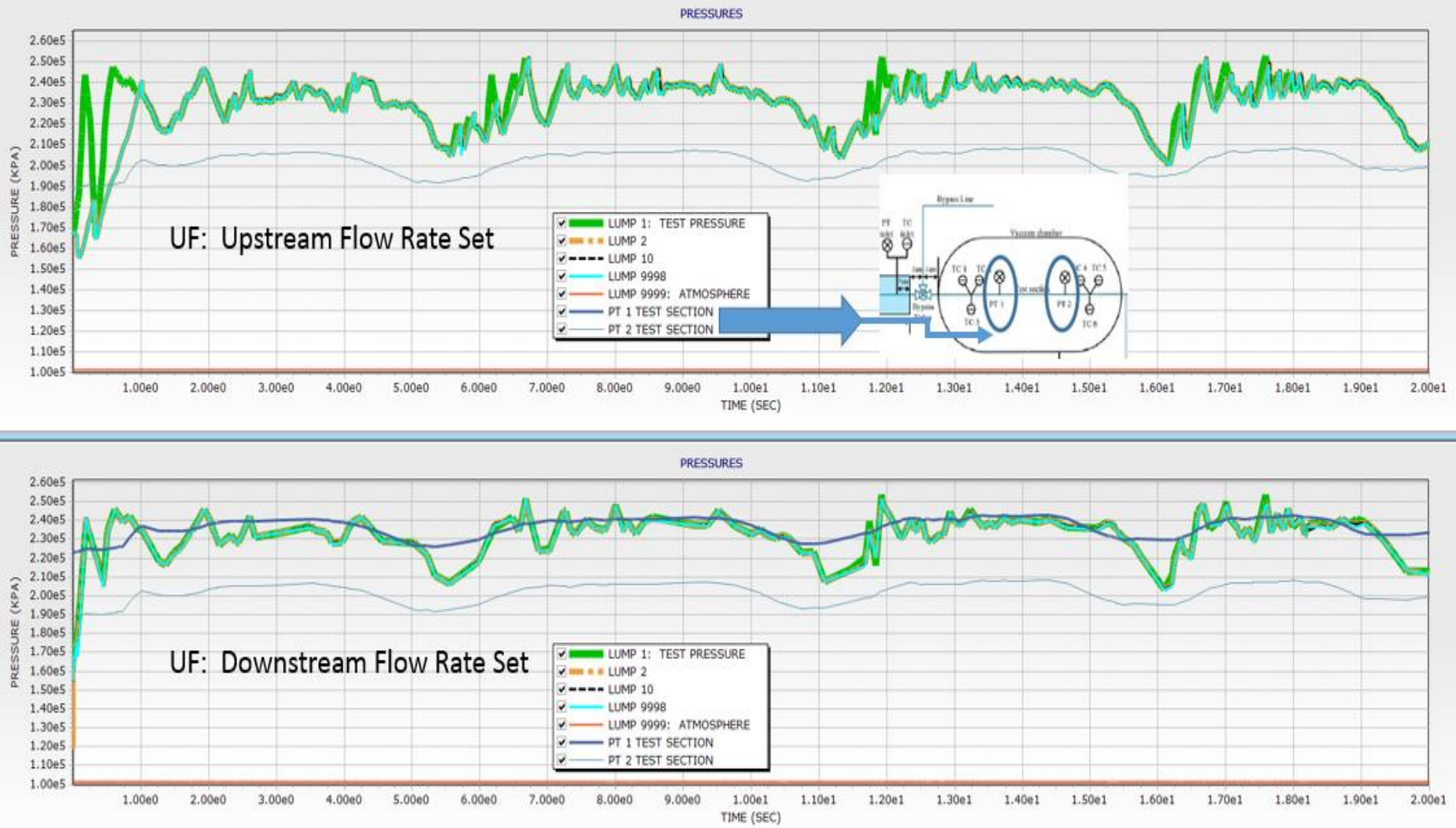
# Liquid Nitrogen Line Chill-down Results (Horizontal Flow)



**Figure 8a-8b: Heat Transfer Coefficient and Wall Temperature for Liquid Nitrogen Horizontal Chill-down Test Case Reynolds Number = 132597**

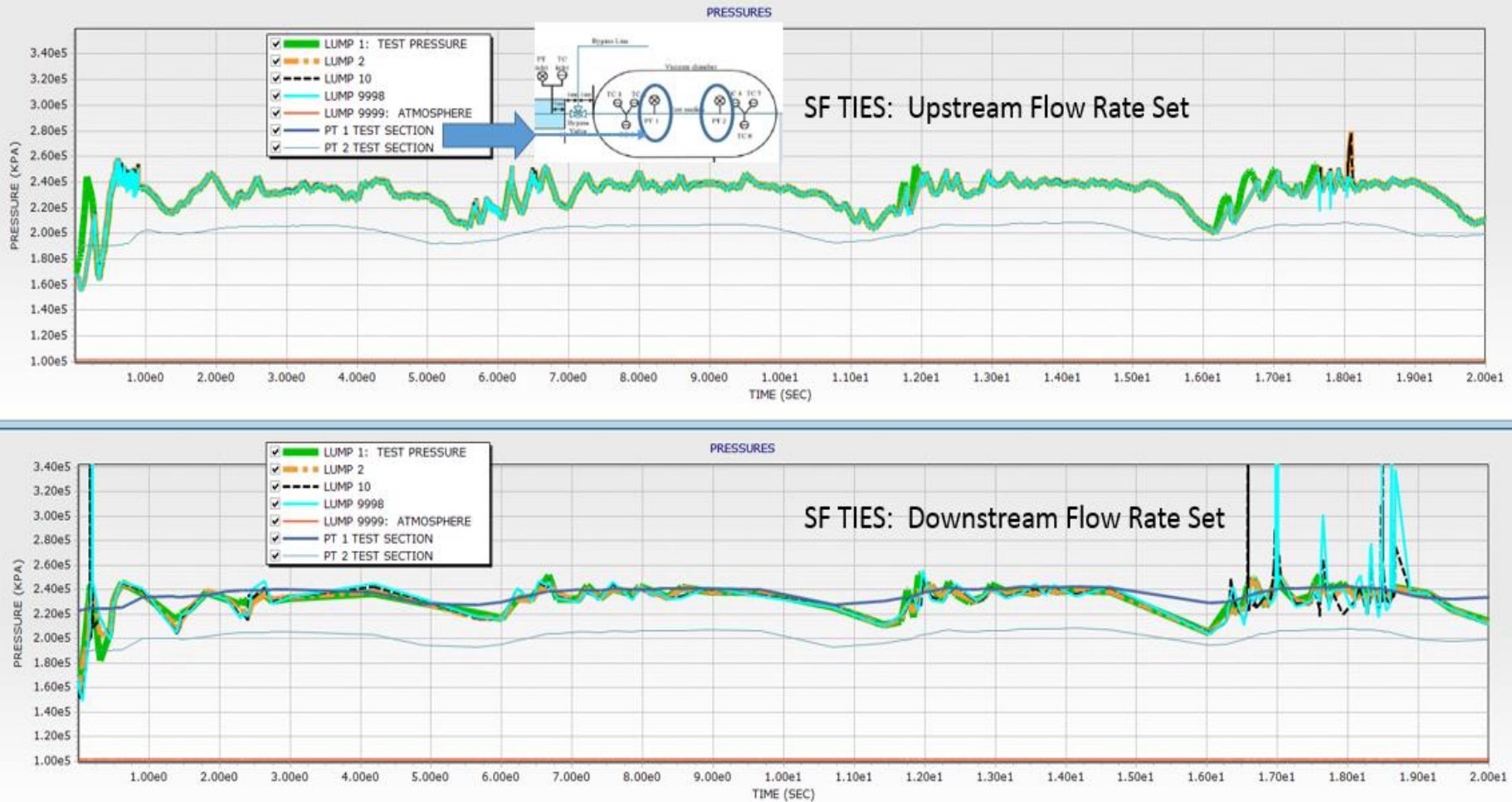


# Liquid Nitrogen Line Chill-down Results (Horizontal Flow)



**Figure 9a-9b: Pressures through the Test Section (Upstream and Downstream Flow Rate Boundaries) for Nitrogen Horizontal Chill-down Test Case Reynolds Number = 23677**

# Liquid Nitrogen Line Chill-down Results (Horizontal Flow)



**Figure 10: Pressures through the Test Section (Upstream and Downstream Flow Rate Boundaries) for Nitrogen Horizontal Chill-down Test Case Reynolds Number = 23677**



# Liquid Nitrogen Line Chill-down Results (Vertical Downward Flow)

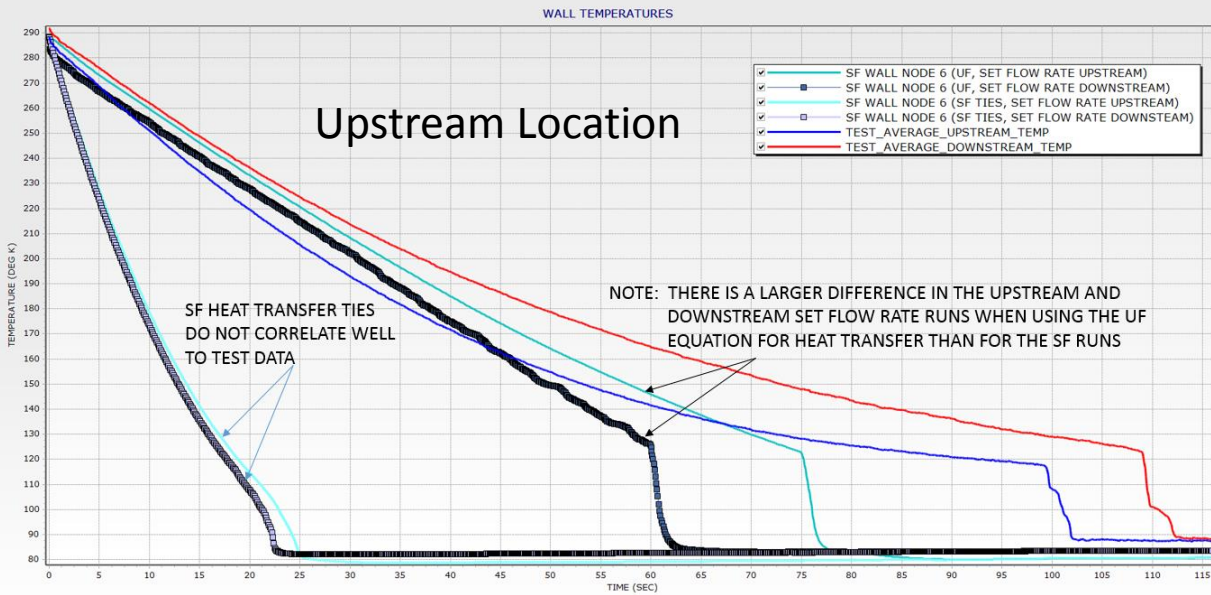
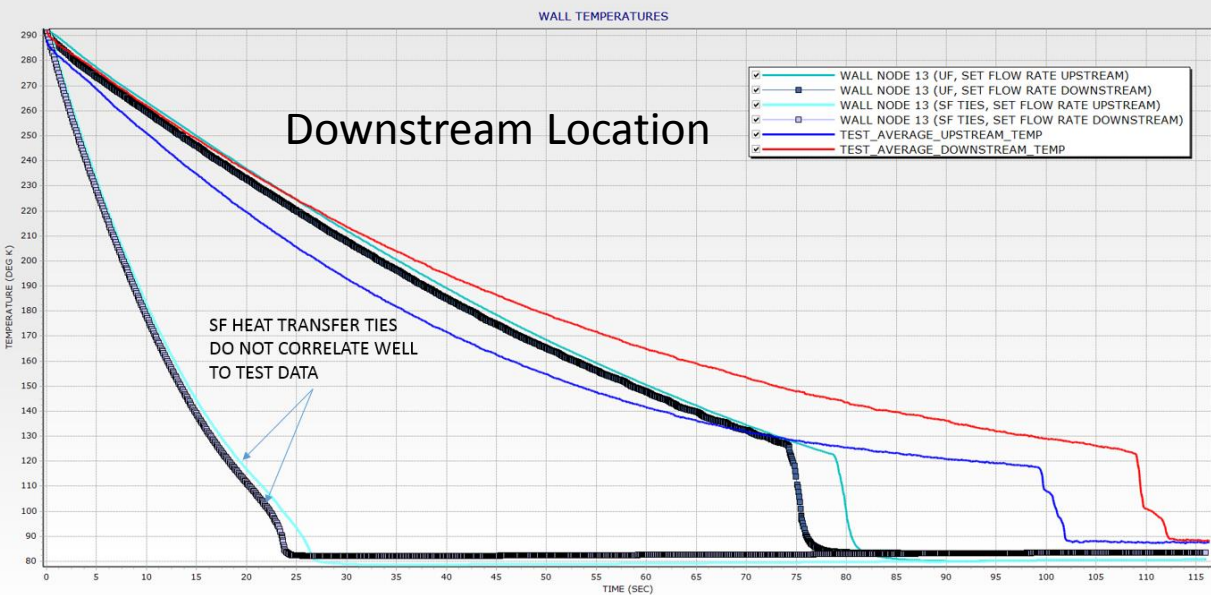
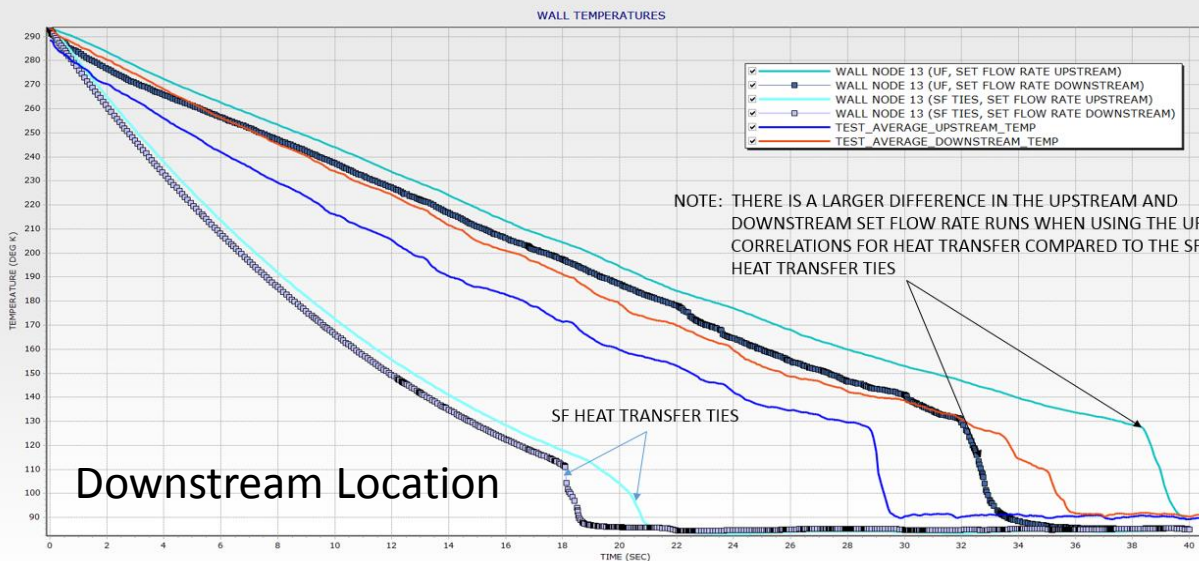
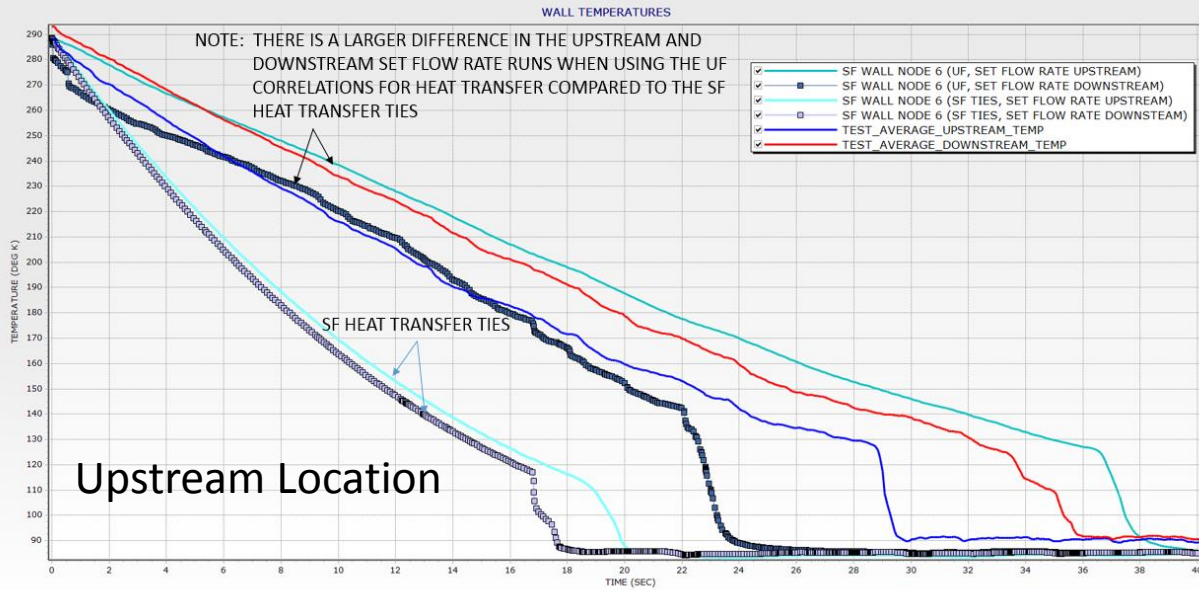


Figure 11a-11b: Wall Temperatures for Liquid Nitrogen Vertical Downward Chill-down Test Case  
Reynolds Number = 4164



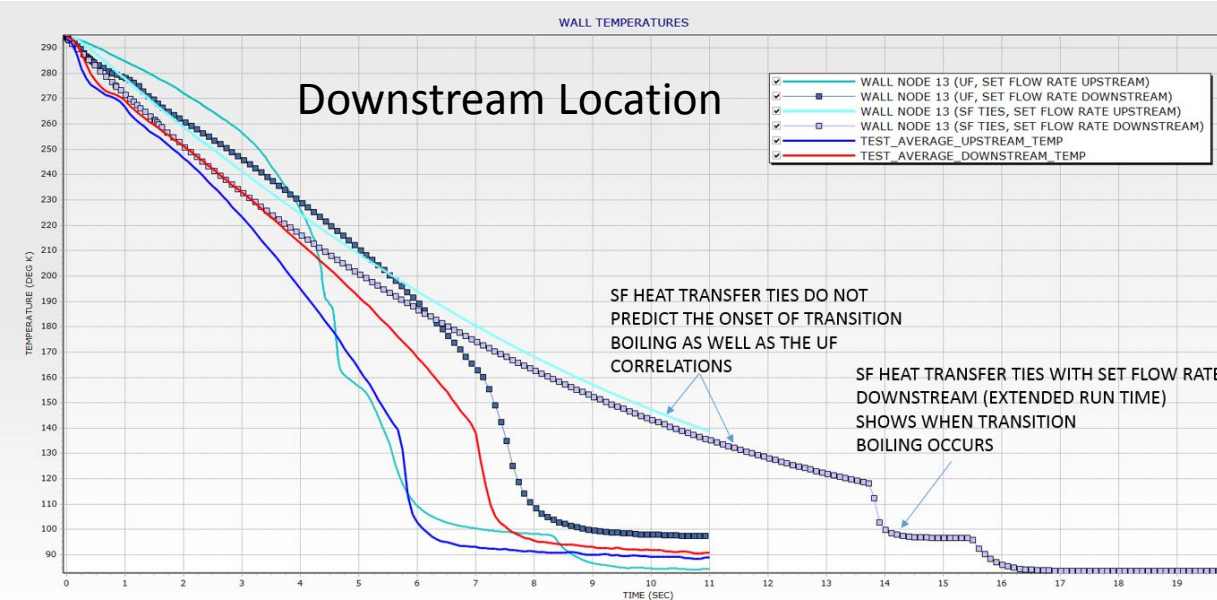
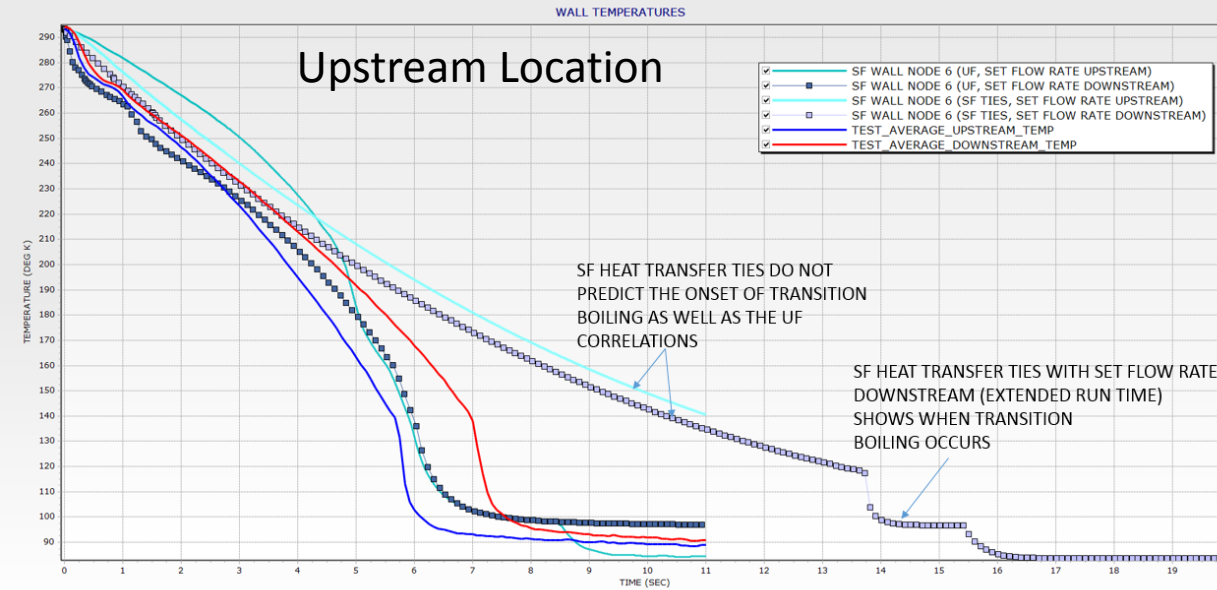
# Liquid Nitrogen Line Chill-down Results (Vertical Downward Flow)



**Figure 12a-b: Wall Temperatures for Liquid Nitrogen Horizontal Chill-down Test Case Reynolds Number = 13350**

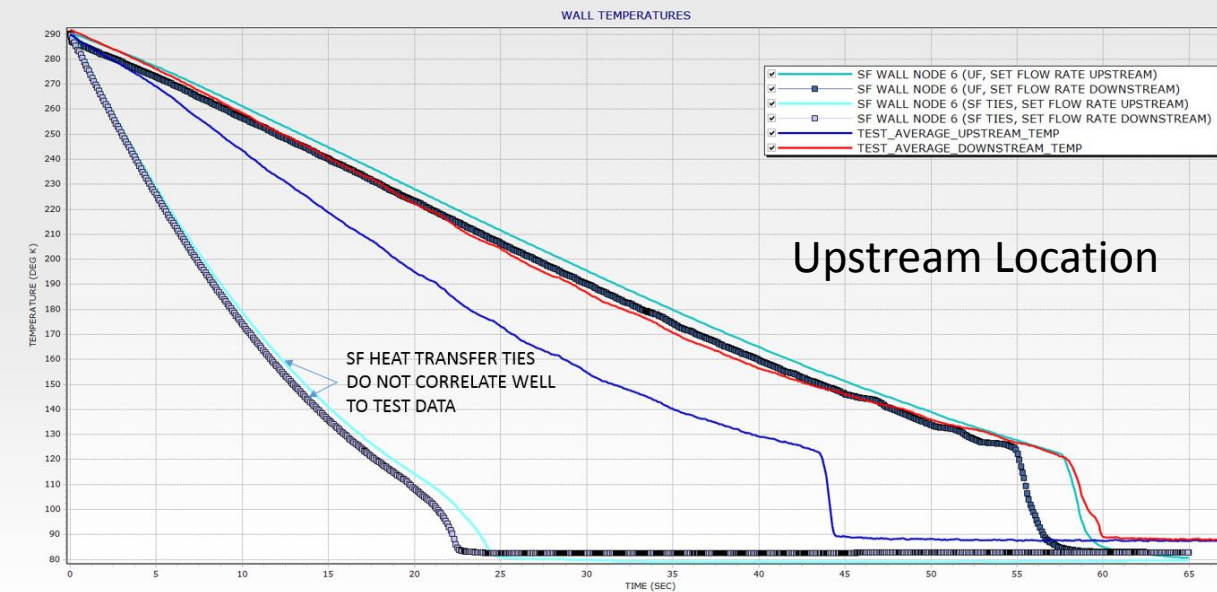


# Liquid Nitrogen Line Chill-down Results (Vertical Downward Flow)



**Figure 13a-b: Wall Temperatures for Liquid Nitrogen Vertical Downward Chill-down Test Case**  
**Reynolds Number = 126423**

# Liquid Nitrogen Line Chill-down Results (Vertical Upward Flow)

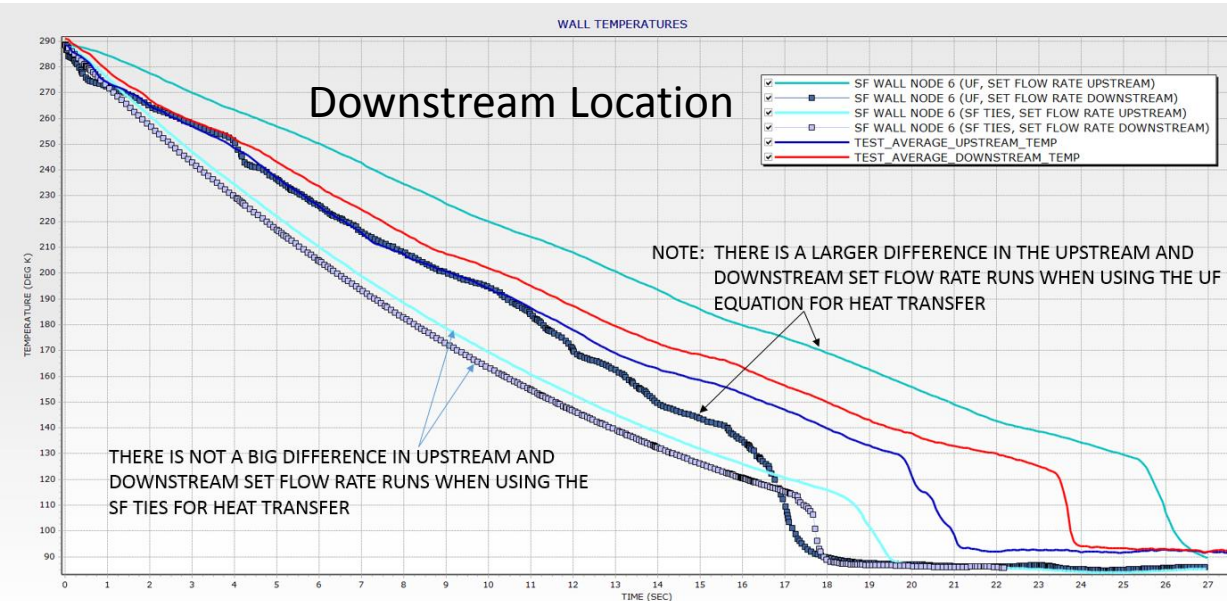
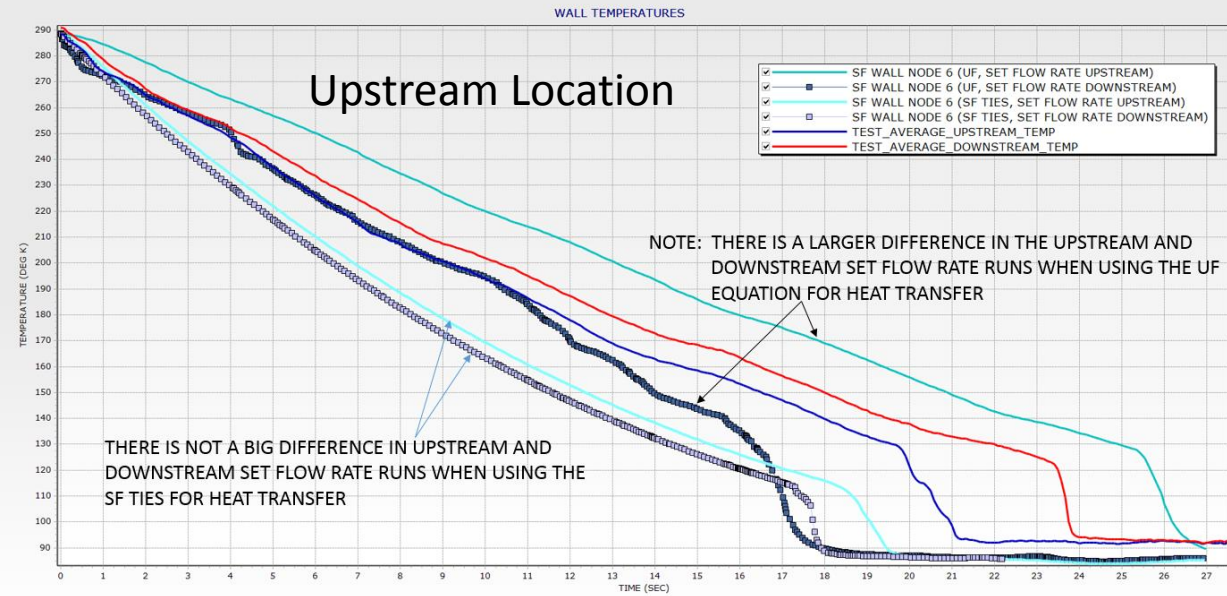


**Figure 14a-b: Wall  
Temperatures for Liquid  
Nitrogen Vertical Upward  
Chill-down Test Case  
Reynolds Number = 3454**





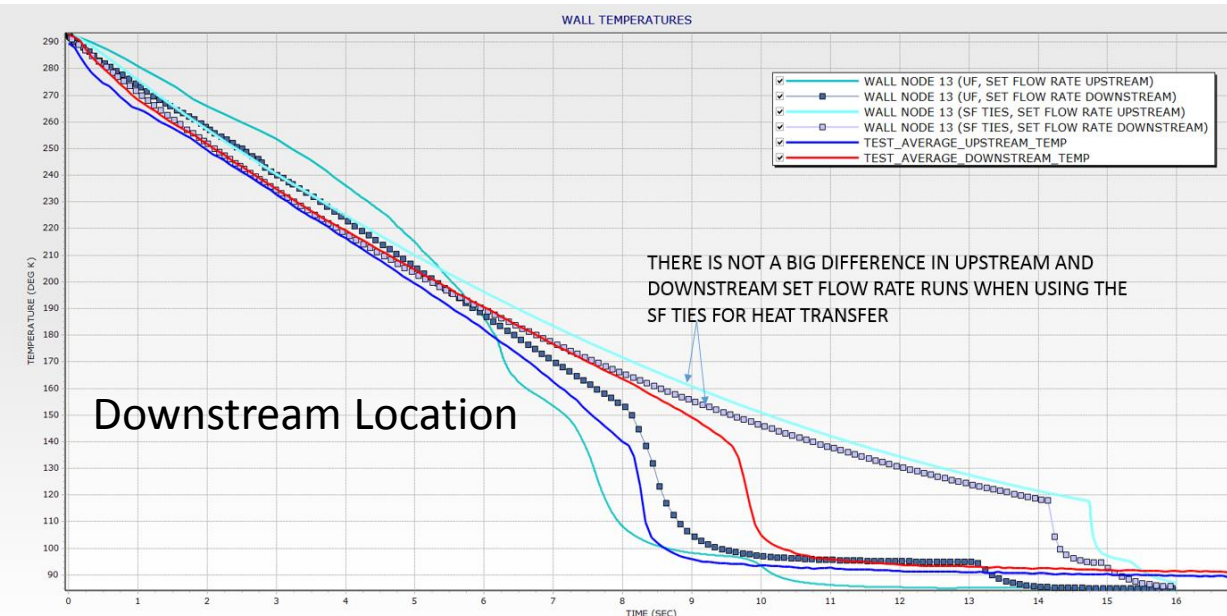
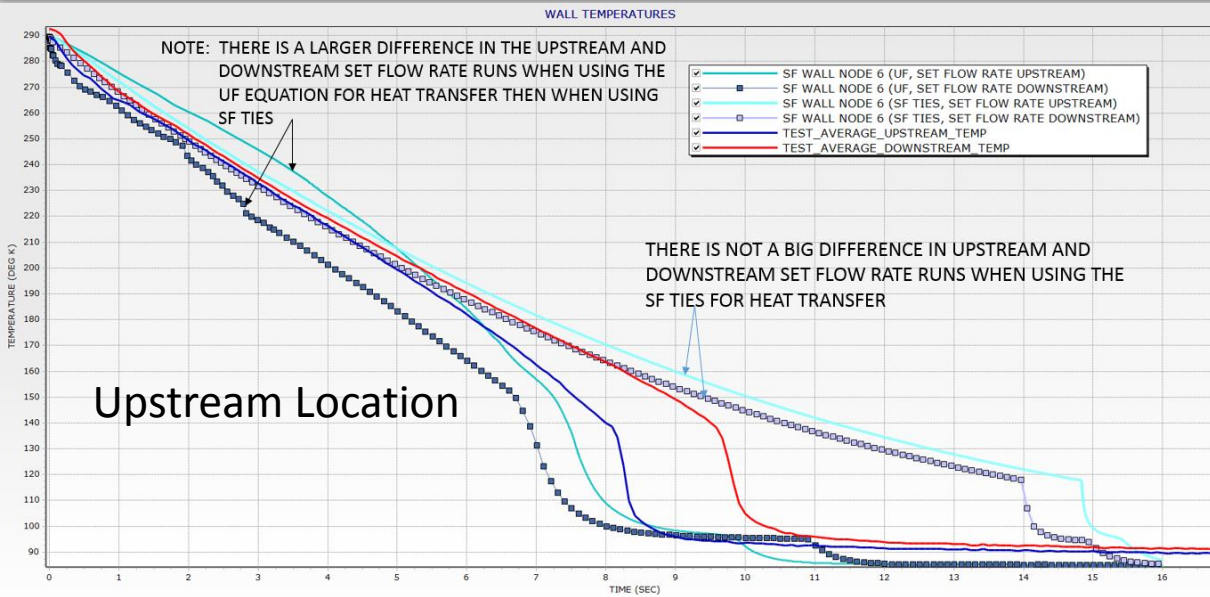
# Liquid Nitrogen Line Chill-down Results (Vertical Upward Flow)



**Figure 15a-b: Wall Temperatures for Liquid Nitrogen Vertical Upward Chill-down Test Case Reynolds Number = 14785**

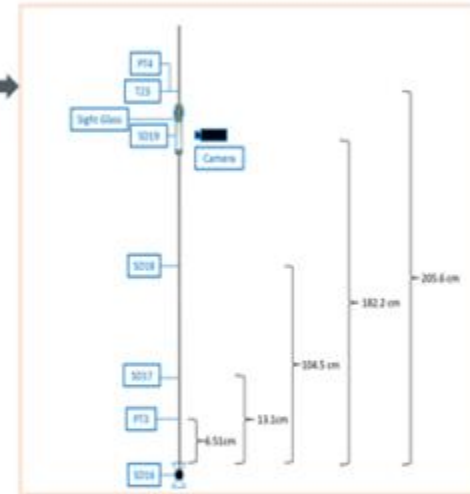
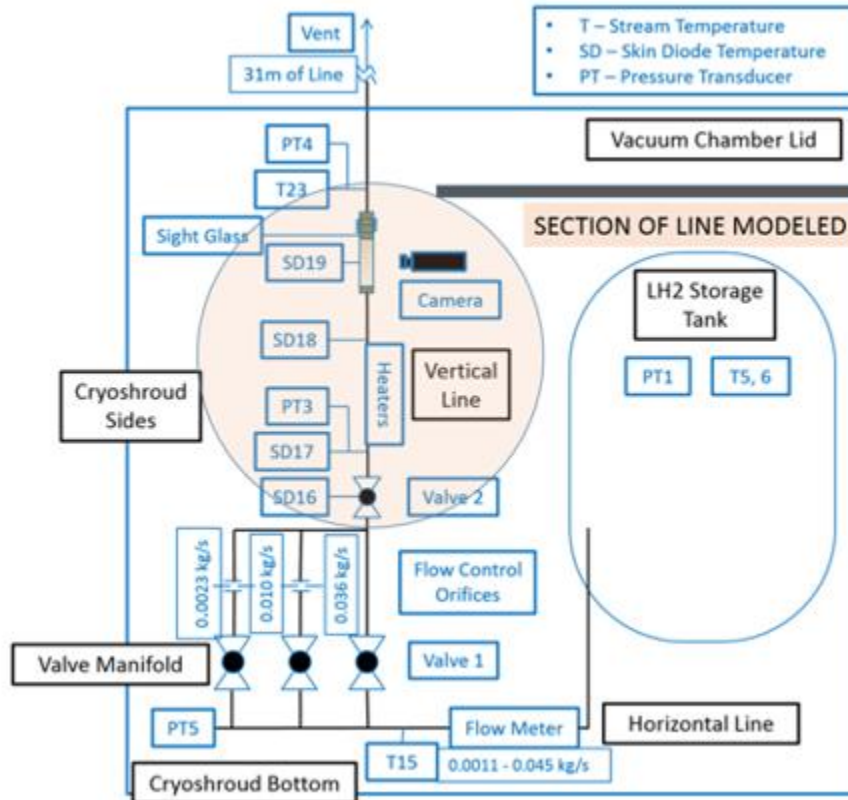


# Liquid Nitrogen Line Chill-down Results (Vertical Upward Flow)



**Figure 16a-b: Wall Temperatures for Liquid Nitrogen Vertical Upward Chill-down Test Case Reynolds Number = 113303**

# Liquid Hydrogen Line Chill-down



Line OD	0.012700025 [m]
Line ID	0.01021 [m]
Length from inlet to skin temperature SD17	0.37148 [m]
Length from inlet to skin temperature SD18	1.285875 [m]
Length from inlet to skin temperature SD19	2.06375 [m]
Length from inlet to stream temperature SD23	2.29 [m]
Length from inlet to P3	0.30798 [m]
Length from inlet to P4	2.29 [m]
Length (approximate) from SD23/P4 to Vent	31 [m]
Total length of straight, vertical section of transfer line	2.29 [m]
Length of SG can/housing	0.15 [m]
Resultant Length of SS pipe	2.14 [m]
Density of 304 SS	8030 [kg/m <sup>3</sup> ]
Mass of flow control manifold (4 orifices, 6 valves, 6 blocks)	11.4 [kg]
Total mass of Sight glass can/housing	1.931818182 [kg]
Effective mass of Sight glass can/housing	0.579545455 [kg]
Mass of SS tubing	0.769925224 [kg]
Total mass of transfer line	4.110743406 [kg]
Total effective mass of vertical transfer line	2.758470678 [kg]

- A set flow rate (from test data) at SD16
- No pressure data at SD16 so the inlet pressure was assumed to be the value taken at location PT3 where the pressure was measured
- Outlet location was PT4 (pressure from test data)
- Since a set inlet flow rate was specified as the boundary condition:
  - PT3 as well as the quality equal to zero were used to determine the thermodynamic state coming into the system

**Figure 17: Liquid Hydrogen Chill-down Test Schematic**

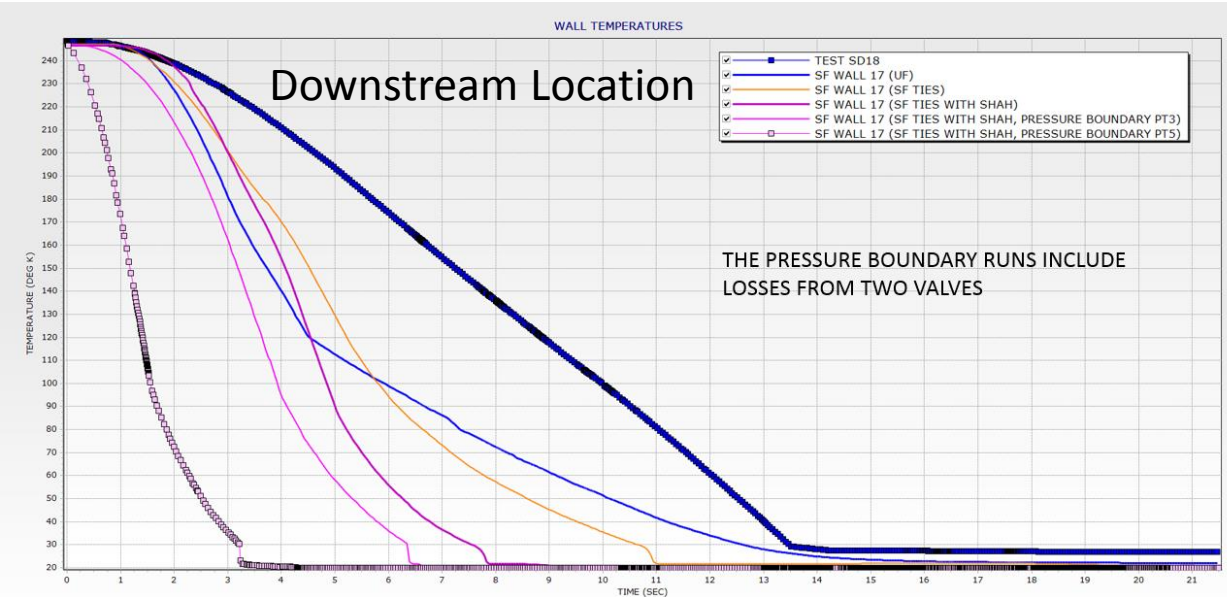
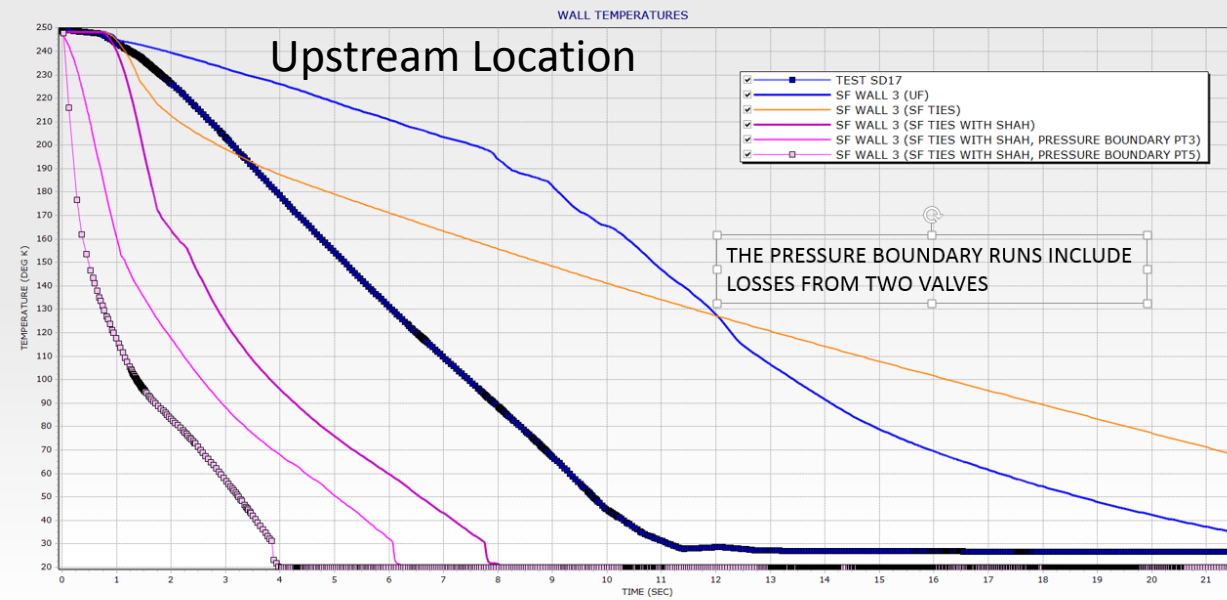
# Liquid Hydrogen Line Chill-down



Figure 18: SINDA/FLUINT Flow Schematic of the Liquid Hydrogen Test Section Showing Fluid LUMPS, Flow PATHS, Wall NODES, Heat Transfer TIES, and Pipe Axial CONDUCTORS



# Liquid Hydrogen Line Chill-down Results (Vertical Upward Flow)



**Figure 19a-b: Wall Temperatures for Liquid Hydrogen Vertical Upward Chill-down Test (Includes Shah Modification for SF TIES, and Pressure Inlet and Outlet Boundary**

Nominal Tank Pressure kPa	T Sat Initial K	LH2 Flow Rate
	207	21.4HIGH

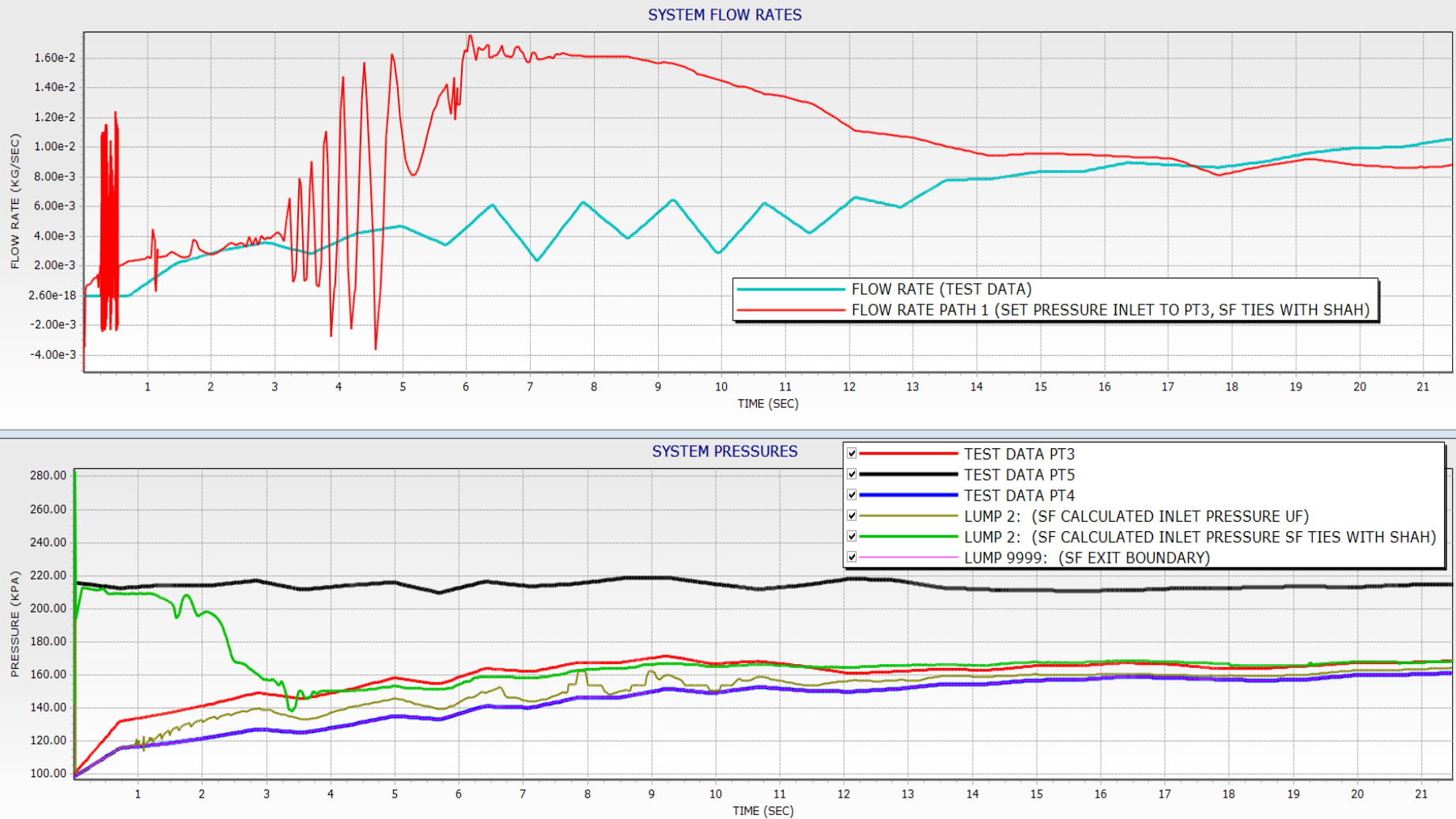
The Shah modification is used during film boiling on the default Dittus-Boelter correlation for gas convective heat transfer as a multiplication factor:

$$S = 0.046 F (T_w/T_w)^{0.55}$$

$$F = 8.53 (L/D)^{-0.63} \quad L/D \leq 30.0$$

$$F = 1.0 \quad L/D \geq 30.0$$

# Liquid Hydrogen Line Chill-down Results (Vertical Upward Flow)



**Figure 20: Flow Rates and Pressure for Liquid Hydrogen Vertical Upward Chill-down (Includes Pressure Inlet and Outlet Boundary)**



# Liquid Hydrogen Line Chill-down Results (Vertical Upward Flow)

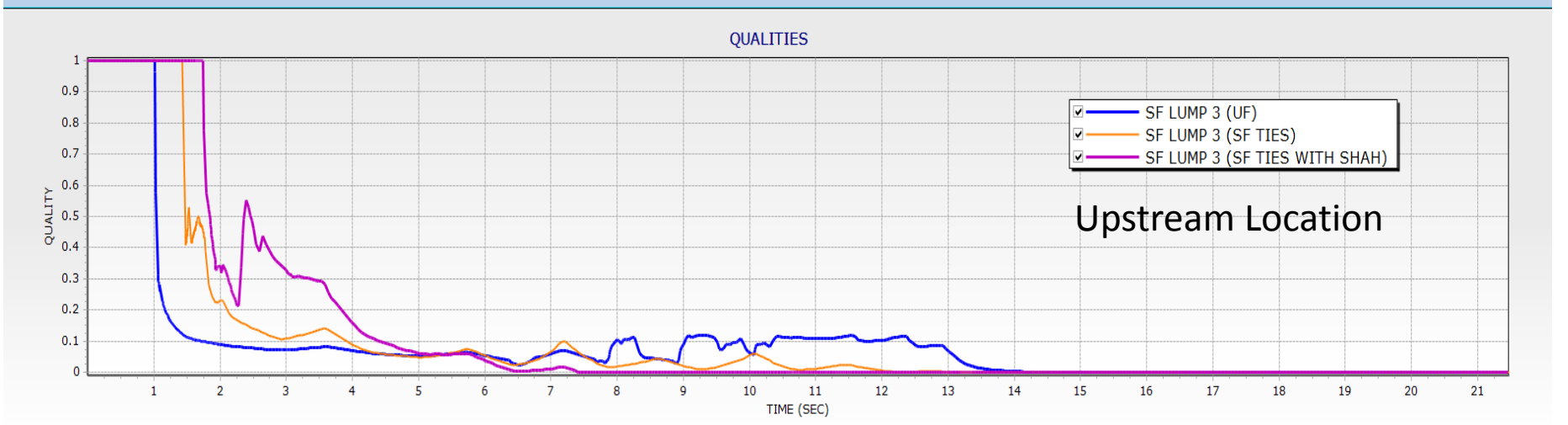
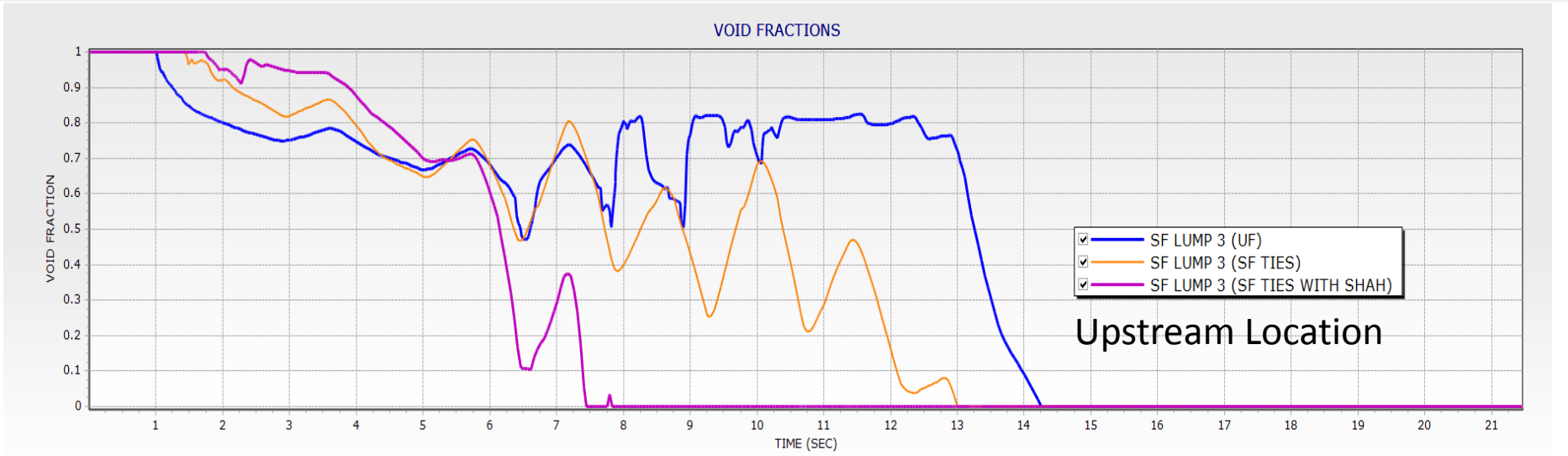
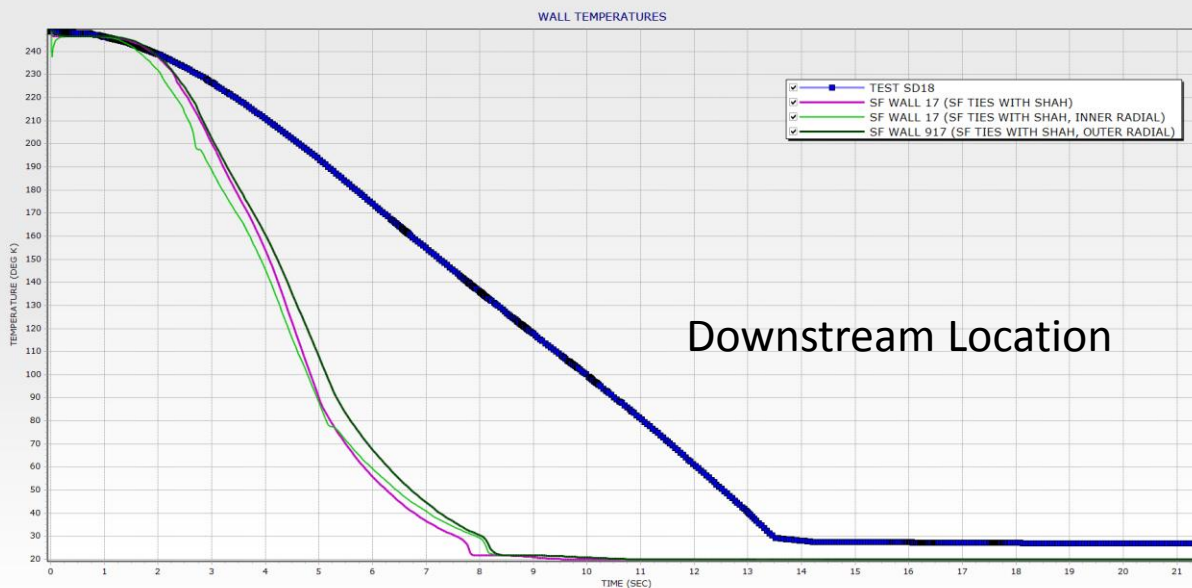
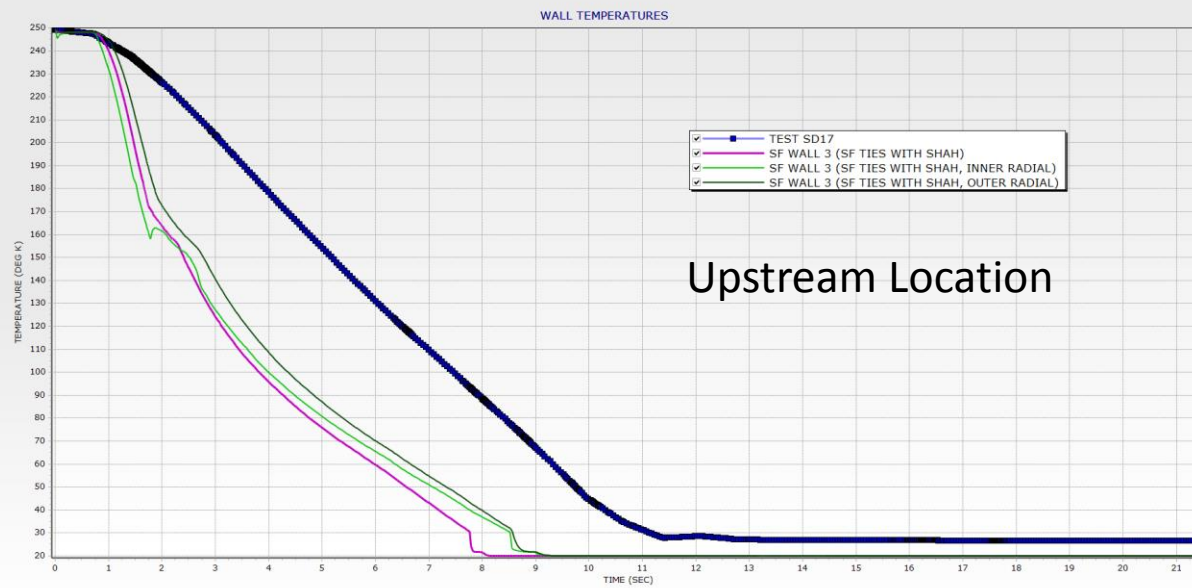


Figure 21: Void Fractions and Qualities for Liquid Hydrogen Vertical Upward Chill-down

Nominal Tank Pressure	T Sat Initial	LH2 Flow
kPa	K	Rate
	207	21.4HIGH

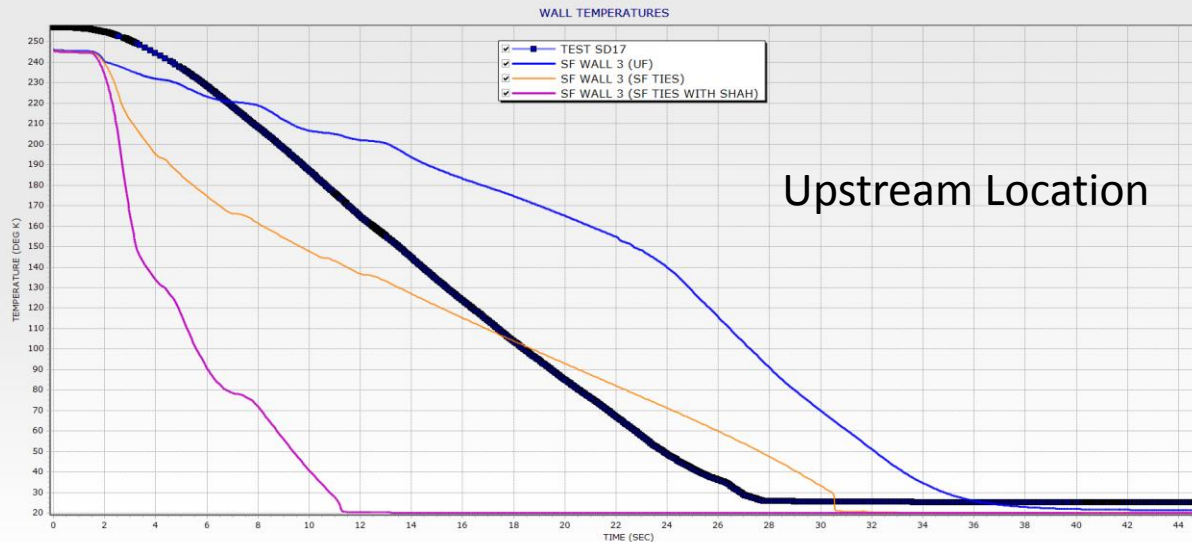
# Liquid Hydrogen Line Chill-down Results (Vertical Upward Flow)



**Figure 22a-b: Inner and Outer Wall Temperatures for Liquid Hydrogen Vertical Upward Chill-down Test (10 Radial Nodes)**

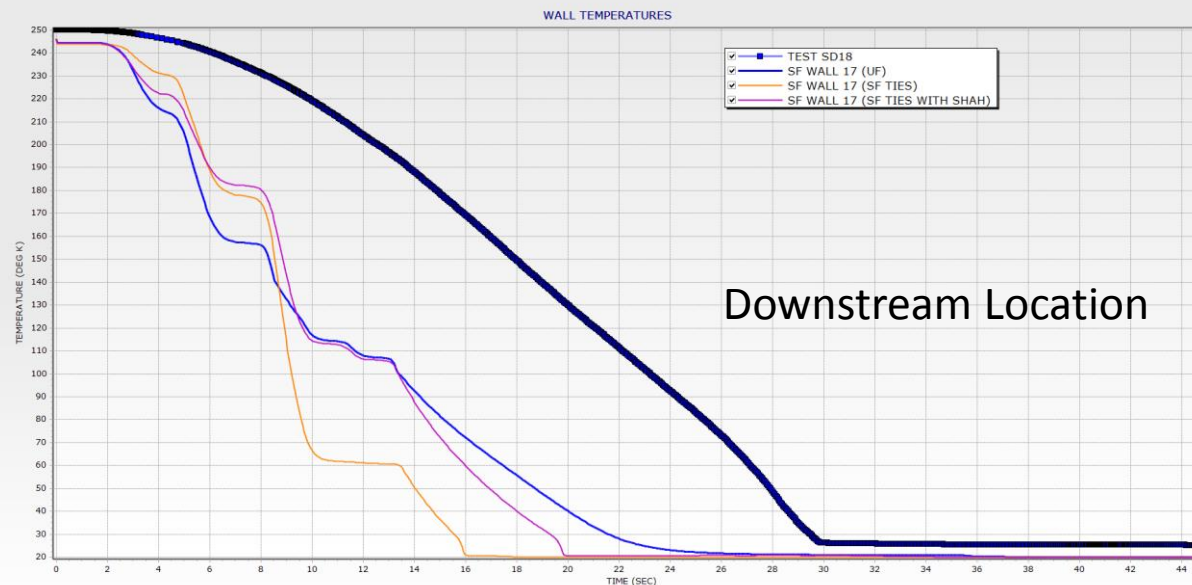
Nominal Tank Pressure kPa	T Sat Initial K	LH2 Flow Rate
	207	21.4HIGH

# Liquid Hydrogen Line Chill-down Results (Vertical Upward Flow)



**Figure 23a-b: Wall Temperatures for Liquid Hydrogen Vertical Upward Chill-down Test (Includes Shah Modification for SF TIES)**

Nominal Tank Pressure kPa	T Sat Initial K	LH2 Flow Rate
	207	21.4MED



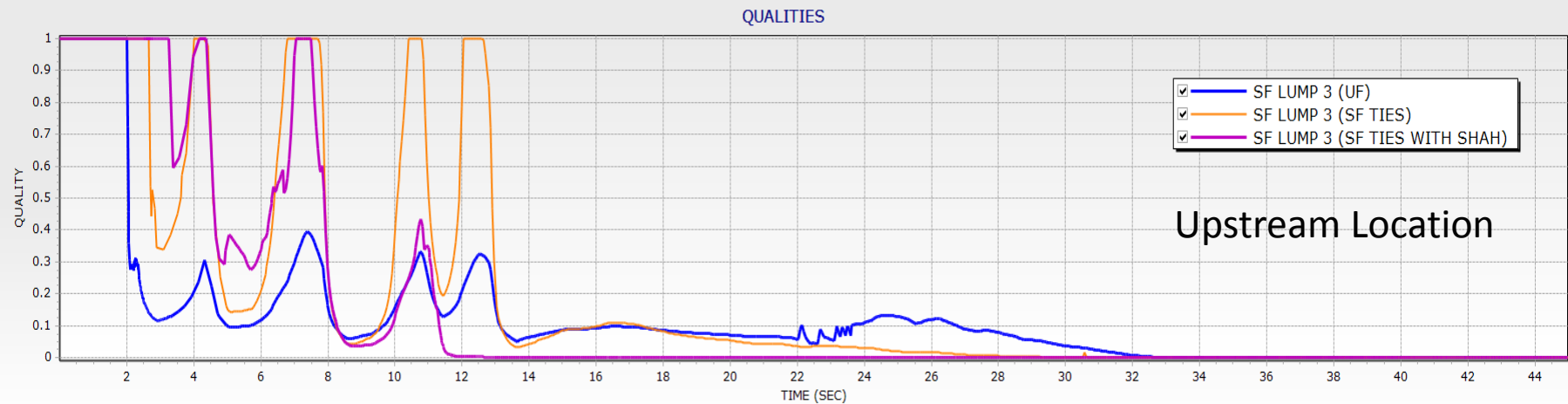
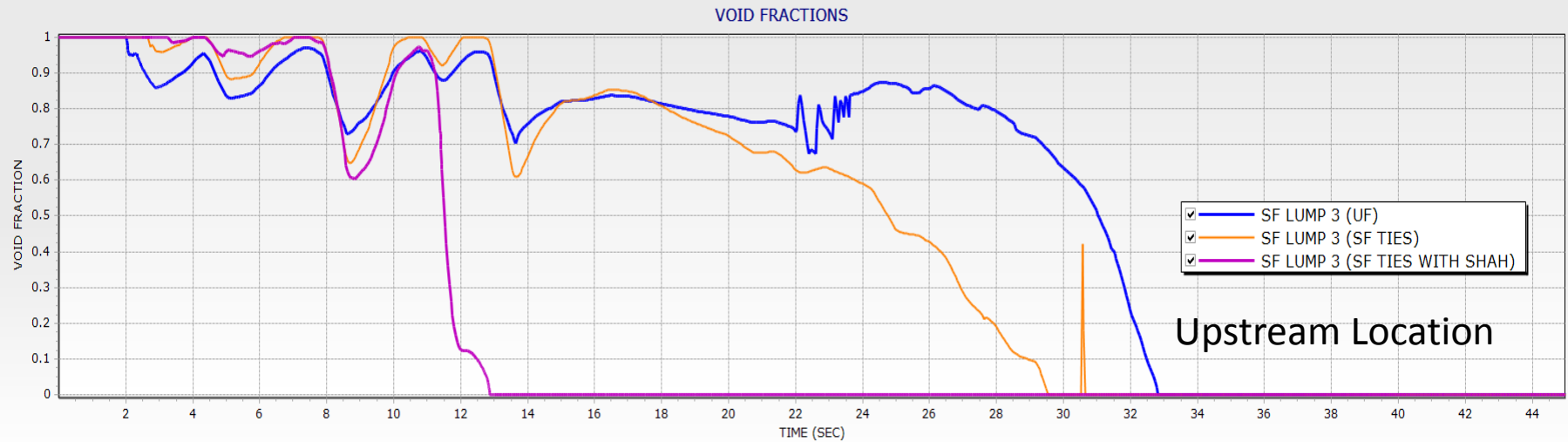
The Shah modification is used during film boiling on the default Dittus-Boelter correlation for gas convective heat transfer as a multiplication factor:

$$S = 0.046 F (T_w/T_w)^{0.55}$$

$$F = 8.53 (L/D)^{-0.63} \quad L/D \leq 30.0$$

$$F = 1.0 \quad L/D \geq 30.0$$

# Liquid Hydrogen Line Chill-down Results (Vertical Upward Flow)

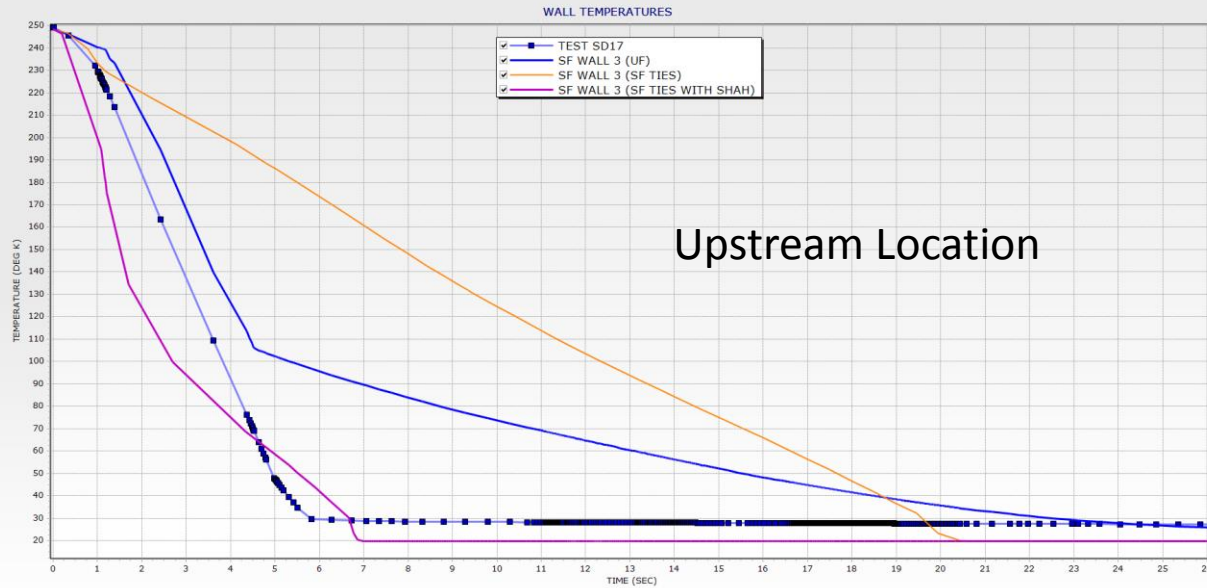


**Figure 24: Void Fractions and Qualities for Liquid Hydrogen Vertical Upward Chill-down**

Nominal Tank Pressure	T Sat Initial	LH2 Flow
kPa	K	Rate
207	21.4MED	

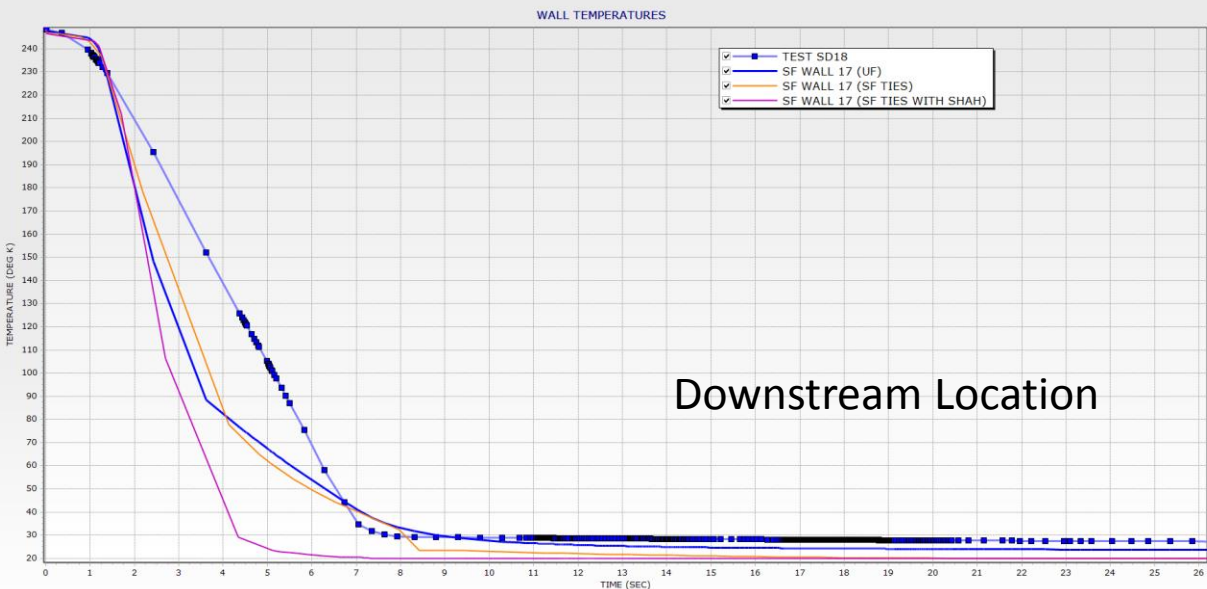


# Liquid Hydrogen Line Chill-down Results (Vertical Upward Flow)



**Figure 25a-b: Wall Temperatures for Liquid Hydrogen Vertical Upward Chill-down Test (Includes Shah Modification for SF TIES)**

Nominal Tank Pressure kPa	T Sat Initial K	LH2 Flow Rate
	345	24.2HIGH



The Shah modification is used during film boiling on the default Dittus-Boelter correlation for gas convective heat transfer as a multiplication factor:

$$S = 0.046 F \left( \frac{T_w}{T_w} \right)^{0.55}$$

$$F = 8.53 (L/D)^{-0.63} \quad L/D \leq 30.0$$

$$F = 1.0 \quad L/D \geq 30.0$$

# Liquid Hydrogen Line Chill-down Results (Vertical Upward Flow)

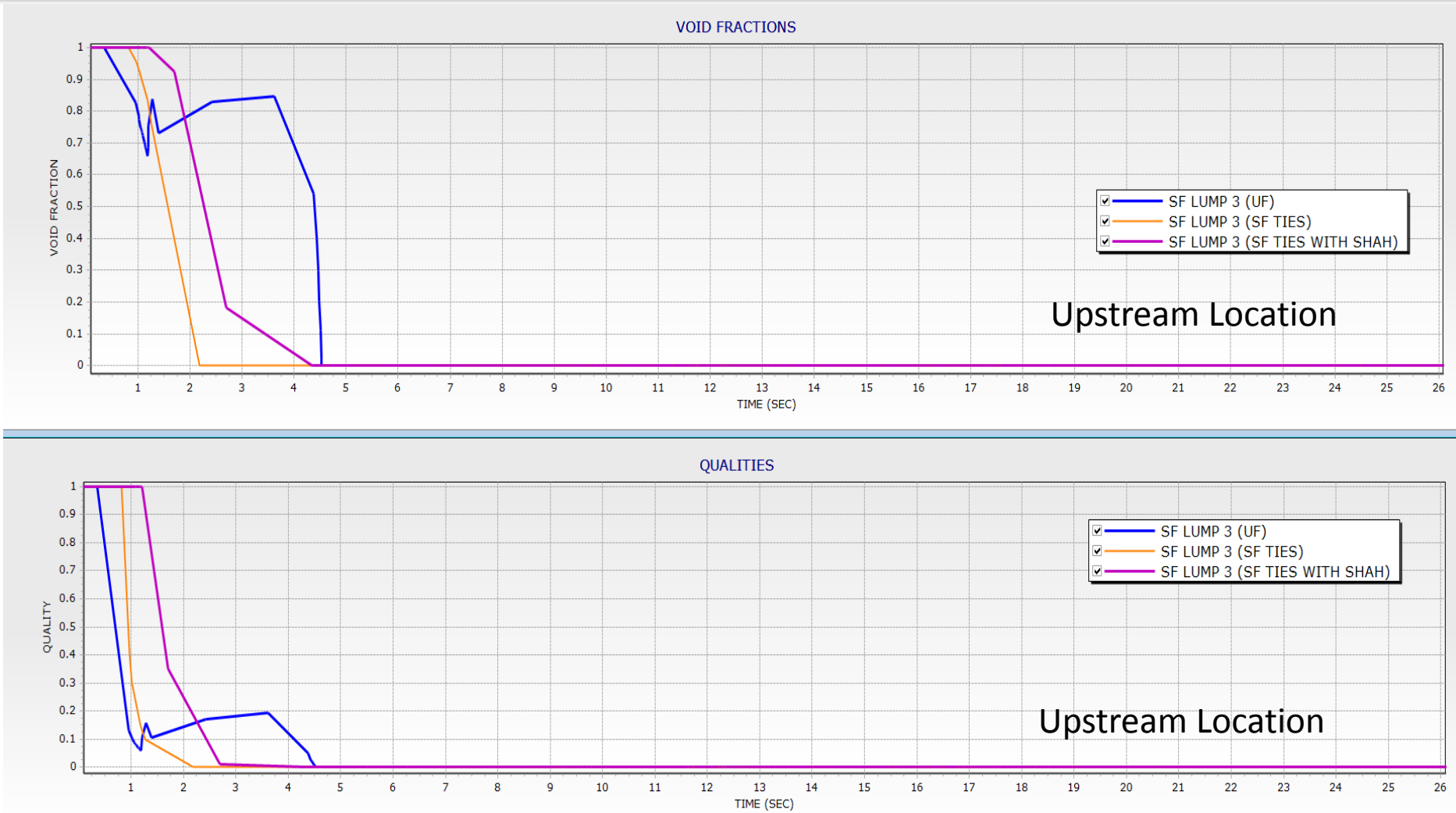
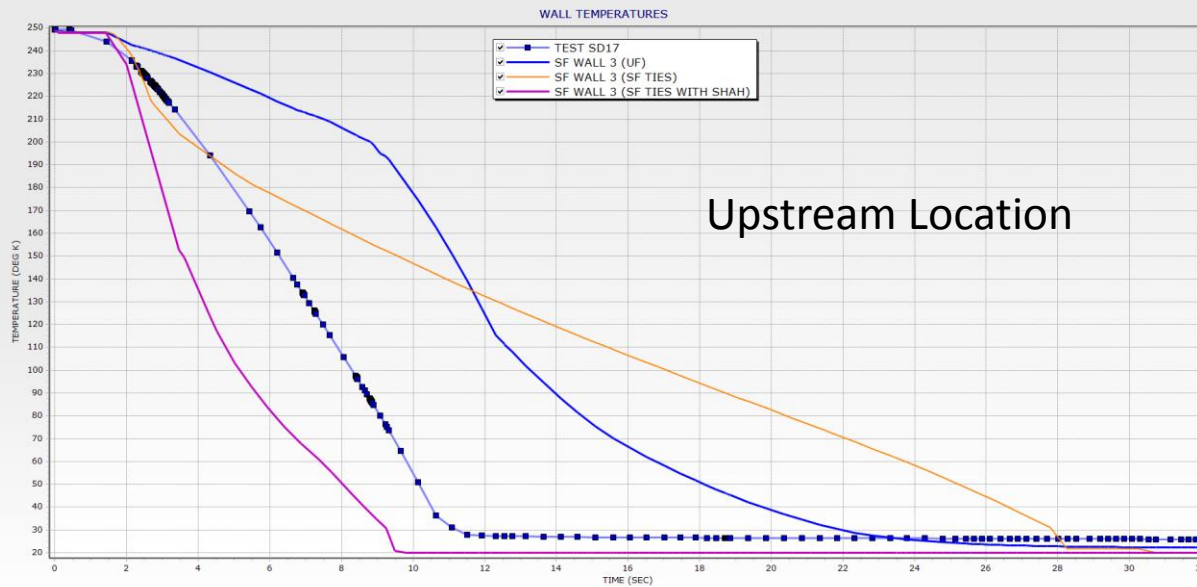


Figure 26: Void Fractions and Qualities for Liquid Hydrogen Vertical Upward Chill-down

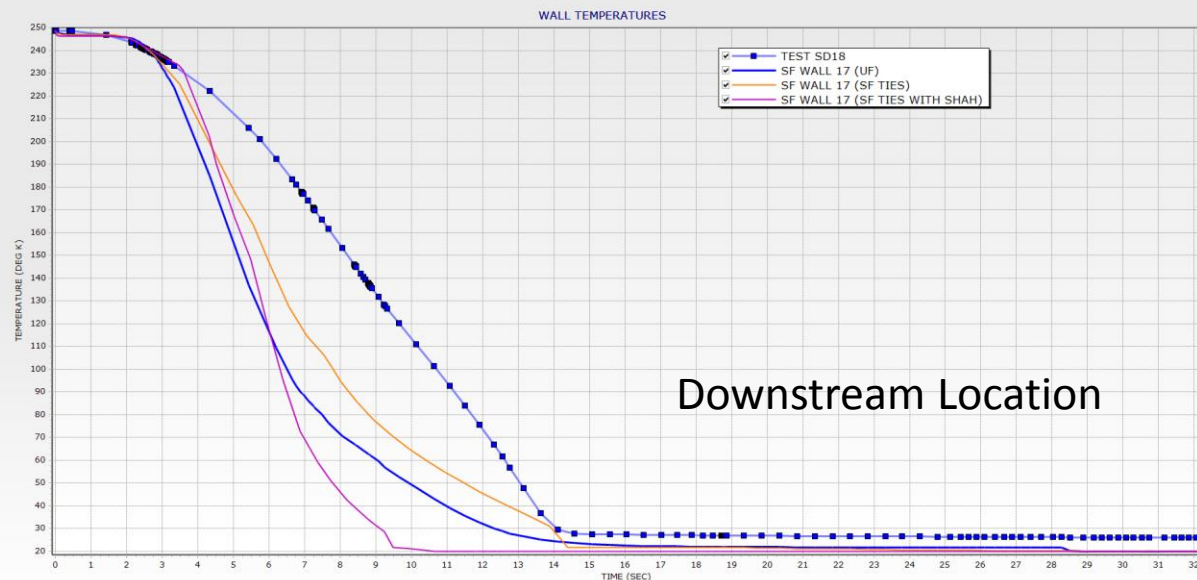
Nominal Tank Pressure	T Sat Initial	LH2 Flow
kPa	K	Rate
	345	24.2HIGH

# Liquid Hydrogen Line Chill-down Results (Vertical Upward Flow)



**Figure 27a-b: Wall Temperatures for Liquid Hydrogen Vertical Upward Chill-down Test (Includes Shah Modification for SF TIES)**

Nominal Tank Pressure kPa	T Sat Initial K	LH2 Flow Rate
345	24.2	MED



The Shah modification is used during film boiling on the default Dittus-Boelter correlation for gas convective heat transfer as a multiplication factor:

$$S = 0.046 F (T_w/T_w)^{0.55}$$

$$F = 8.53 (L/D)^{-0.63} \quad L/D \leq 30.0$$

$$F = 1.0 \quad L/D \geq 30.0$$

# Liquid Hydrogen Line Chill-down Results (Vertical Upward Flow)

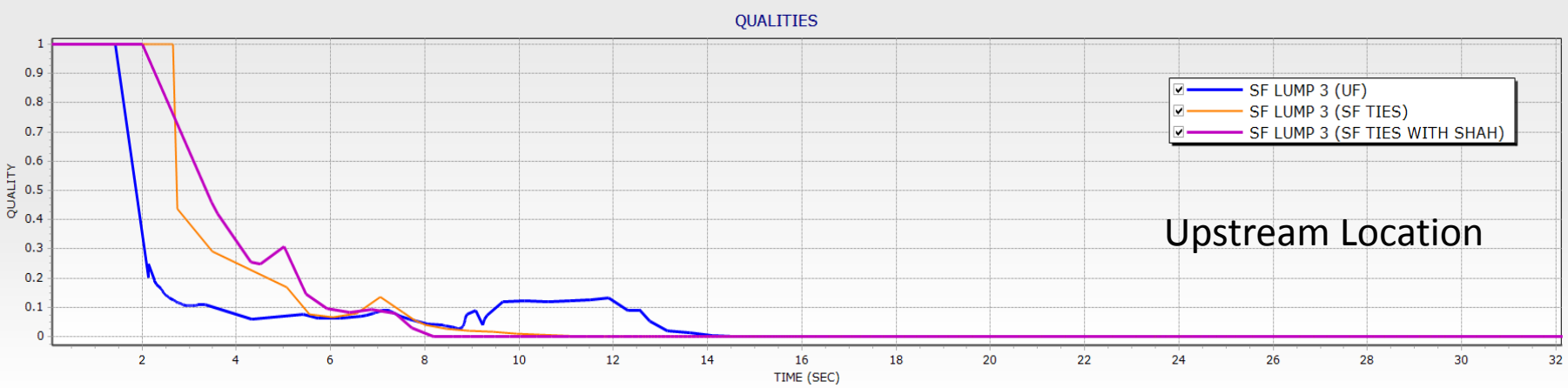
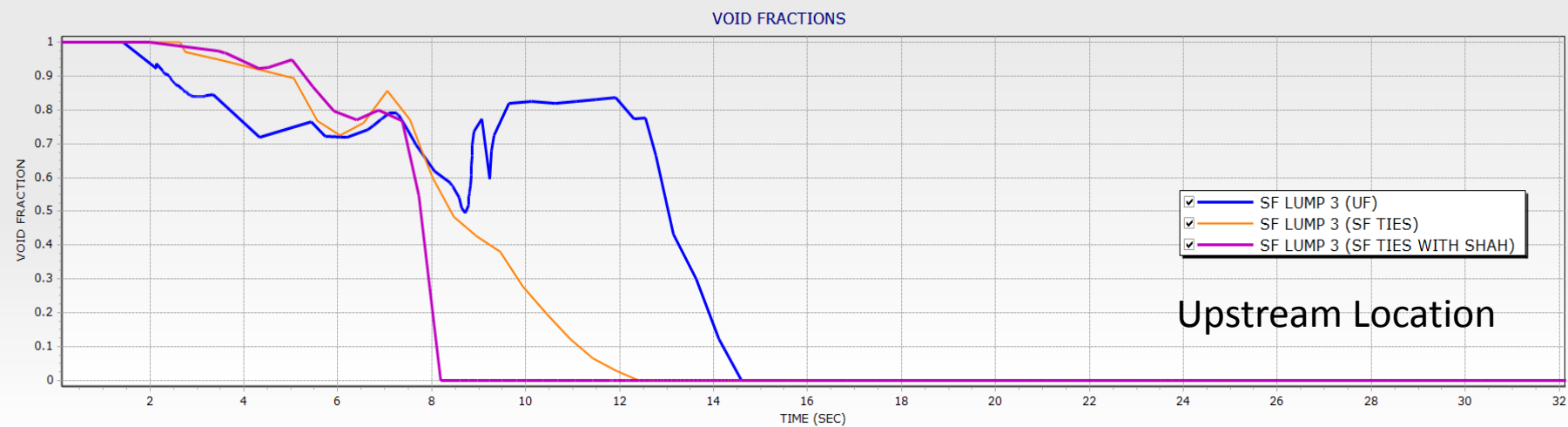


Figure 28: Void Fractions and Qualities for Liquid Hydrogen Vertical Upward Chill-down

Nominal Tank Pressure	T Sat Initial	LH2 Flow
kPa	K	Rate
	345	24.2MED



- University of Florida's film boiling correlation can over predict heat transfer to the wall due to flow rate oscillations
- SINDA/FLUINT's correlations can either over predict or under predict the film boiling heat transfer to the wall, but is less sensitive to flow rate oscillations
  - high Reynolds numbers under predict film boiling ( $\sim 100000$ )
  - low Reynolds numbers over predict film boiling ( $\sim 5000$ )
  - Reynolds number ( $\sim 10000$ ) "just about right"
- Along with heat transfer correlations for multiphase flow, pressure drop correlations need to be addressed and/or modified since the pressure drops in all the cases did not correlate to test data, whether upstream or downstream set flow rates were employed

- Test cases with hydrogen showed that radially discretizing the wall did not significantly impact the model temperature results
- Sometime SINDA/FLUINT did better, other times the UF correlations faired better